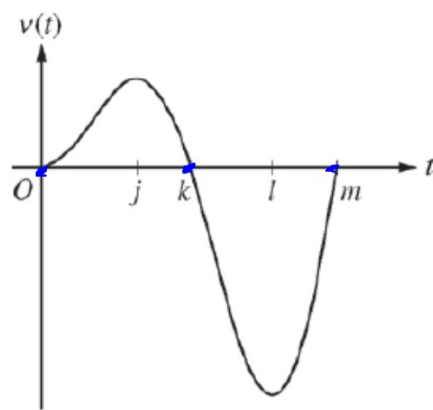


Motion on a line (Interpreting  $f'$ (velocity) graphs)

## I. Review: Motion Along A Line

If  $x(t)$  represents the position of a particle along the  $x$ -axis at any time  $t$ , then the following statements are true.

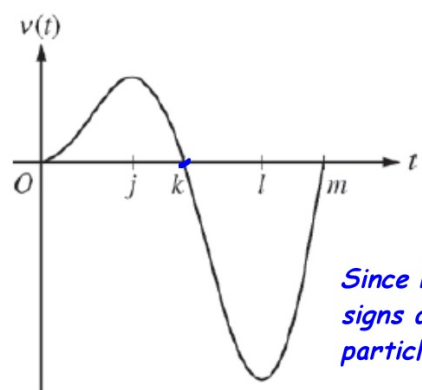
1. "Initially" means \_\_\_\_\_ = 0.
2. "At rest" means \_\_\_\_\_ = 0.
3. If the velocity of the particle is positive, then the particle is moving to the \_\_\_\_\_.
4. If the velocity of the particle is \_\_\_\_\_, then the particle is moving to the left.
5. To find average velocity over a time interval, divide the change in \_\_\_\_\_ by the change in time.
6. Instantaneous velocity is the velocity at a single moment or \_\_\_\_\_ in time.
7. If the acceleration of the particle is positive, then \_\_\_\_\_ is increasing.
8. If the acceleration of the particle is \_\_\_\_\_, then the velocity is decreasing.
9. In order for a particle to change direction, the \_\_\_\_\_ must change signs.
10. Speed is the \_\_\_\_\_ of velocity.



$[0, m]$

1) State the value(s) of  $t$  where the particle is at rest.

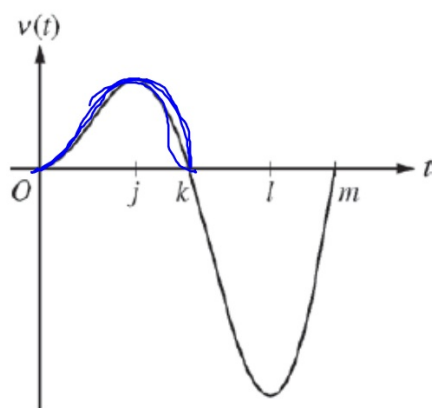
$$t = 0, k, m$$



*Since  $k$  is zero and  $v(t)$  changes signs at  $t = k$ , this is where the particle changes direction*

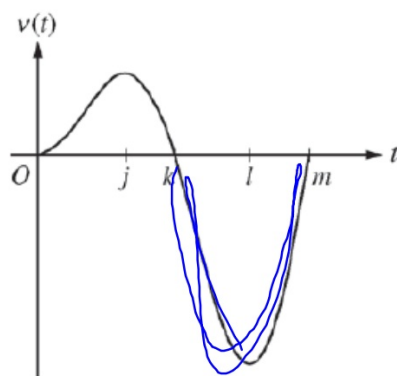
2) State the value(s) of  $t$  where the particle is changing direction.  $t = k$

$$v(t) > 0$$

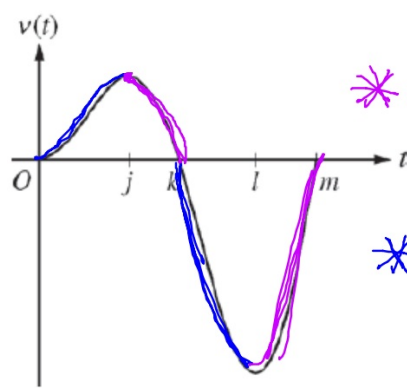


3) State the interval(s) where the particle is moving to the right.  $(0, k)$

$$v(t) < 0$$



4) State the interval(s) where the particle is moving to the left.  $(k, m)$

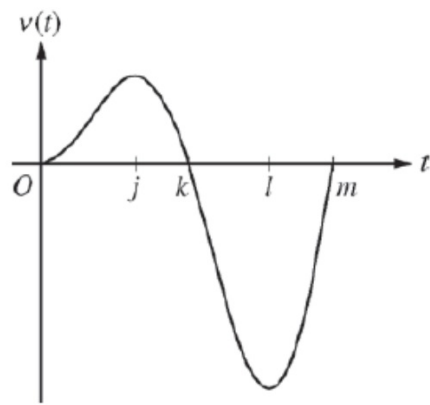


\* *Slowing down:*  
 *$v(t)$  and  $a(t)$  have*  
*opposite signs.  $(j, k) \cup (l, m)$*

\* *Speeding up:*  
 *$v(t)$  and  $a(t)$*   
*same signs.  $(0, j) \cup (k, l)$*

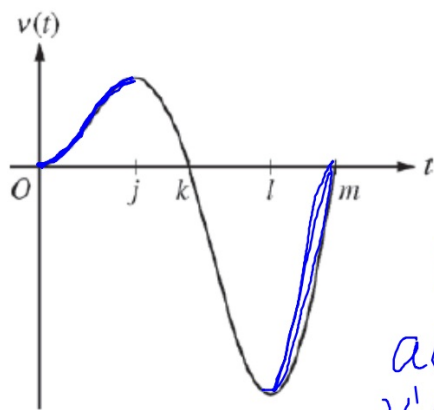


5) State the interval(s) where the particle is slowing down and speeding up.



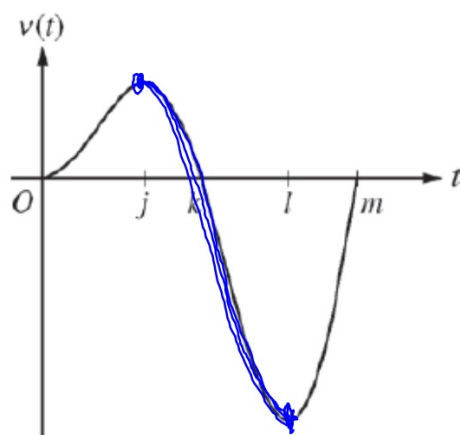
6) State the interval(s) where the particle is speeding up.





$(0, j) \cup (l, m)$   
 $a(t) > 0$   
 $v'(t) > 0$

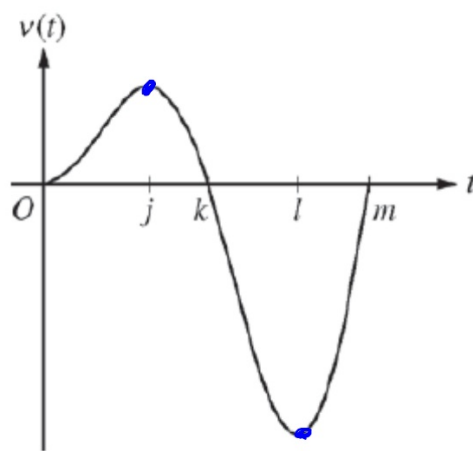
- 7) State the interval(s) where the velocity is increasing.  
 (acceleration is positive)  
 (slope of  $v(t)$ )



$a(t) < 0$   
 (acceleration is negative  
 or slope of velocity is  
 negative)

$(j, l)$   
 slope of  $v(t) < 0$  ✓

8) State the interval(s) where the velocity is decreasing.



$j, l$   
because  
slope of  $v(t)$   
is changing signs  
at these points.

9) At what time(s) is the acceleration zero?

2. Analytical (NO CALCULATOR)

A particle moves along the x-axis so that at any time  $t$  its position is given by:

$$x(t) = t^3 - 6t^2 + 9t + 11$$

b) At  $t=1$ , is the velocity of the particle increasing or decreasing? JYA.

$$x'(t) = 3t^2 - 12t + 9$$

$$x''(t) = 6t - 12$$

$$x''(1) = -6$$

*Decreasing because*  
 $a(1) < 0$

$$a(t) < 0 \text{ at } t=1$$

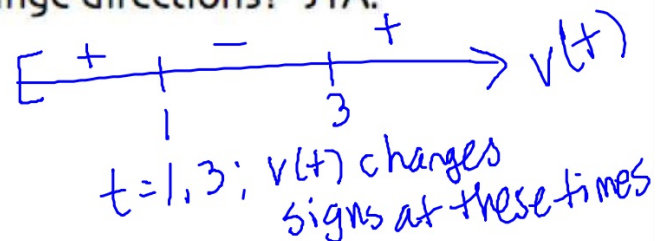
2. Analytical (NO CALCULATOR)

A particle moves along the x-axis so that at any time  $t$  its position is given by:

$$x(t) = t^3 - 6t^2 + 9t + 11$$

d) At what time does the particle change directions? JYA.

$$\begin{aligned}x'(t) &= 3t^2 - 12t + 9 \\ &= 3(t^2 - 4t + 3) \\ &= 3(t-3)(t-1)\end{aligned}$$



2. Analytical (NO CALCULATOR)

A particle moves along the x-axis so that at any time  $t$  its position is given by:

$$x(t) = t^3 - 6t^2 + 9t + 11$$

e) At  $t=5$ , is the speed of the particle increasing or decreasing? JYA.

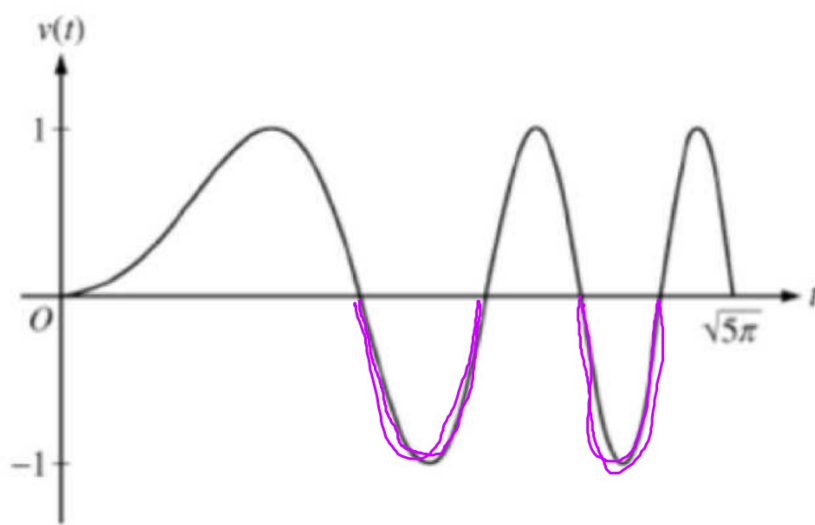
$$v(5) > 0$$

$$a(5) > 0$$

$v(5)$  and  $a(5)$  have  
the same sign  $\therefore$   
the speed is increasing.

HW: 6 (CALCULATOR)

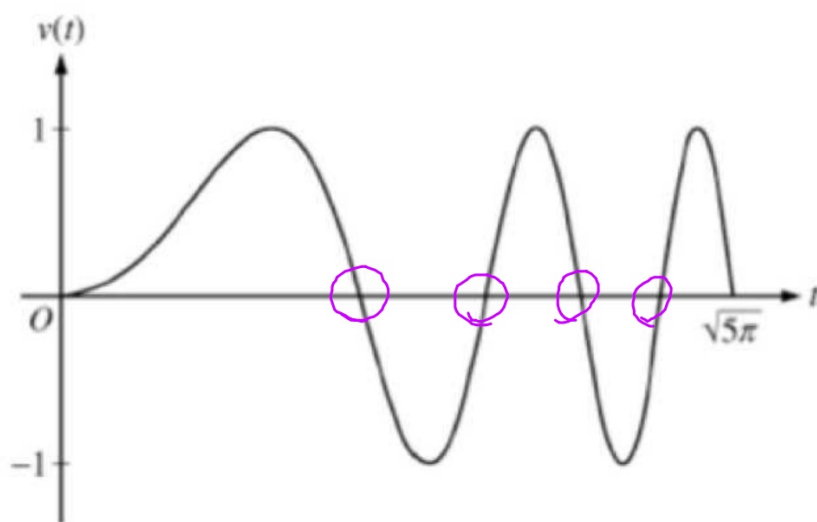
3 decimal places



$$v(t) = \sin(t^2)$$

a) When is the particle moving to the left? JYA.

HW: 6 (CALCULATOR)

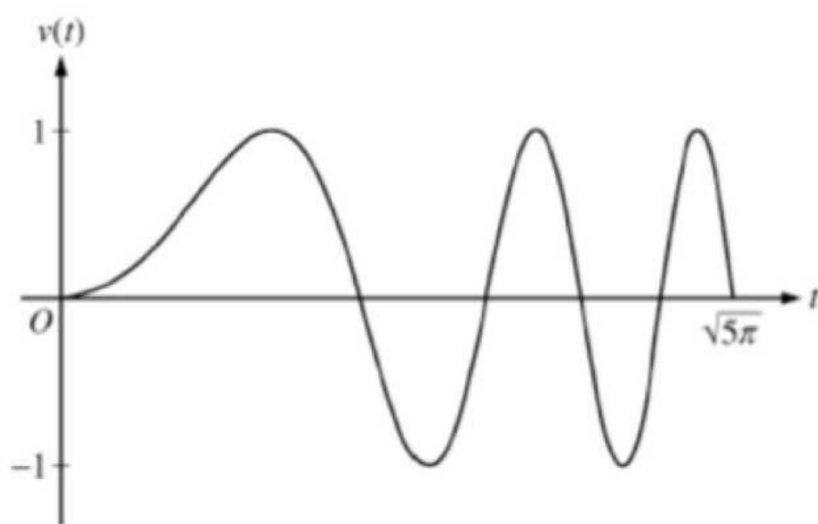


$$v(t) = \sin(t^2)$$

e) When does the particle change direction? JYA.



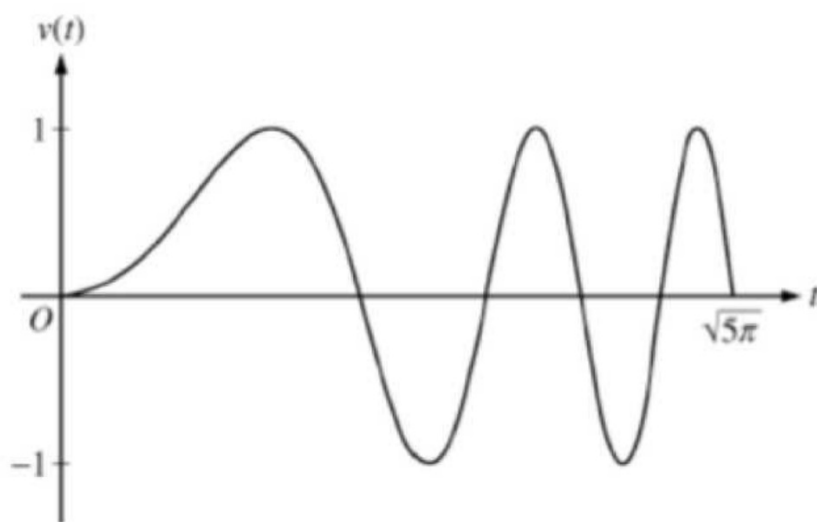
HW: 6 (CALCULATOR)



$$v(t) = \sin(t^2)$$

c) Is the particle slowing down at  $t = 1.5$ ? Explain.

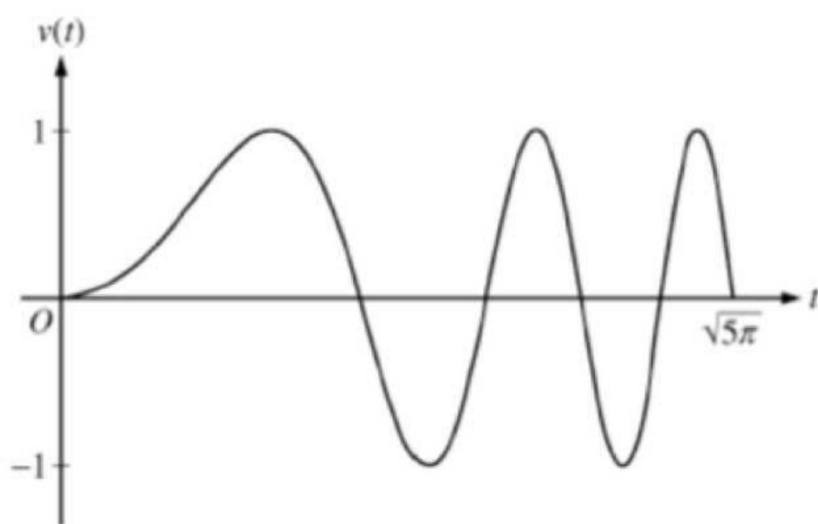
HW: 6 (CALCULATOR)



$$v(t) = \sin(t^2)$$

d) Is the particle speeding up at  $t = 2.4$ ? Explain.

HW: 6 (CALCULATOR)



$$v(t) = \sin(t^2)$$

f) What is the average acceleration on the interval  $[1, 4]$ ?

*Curve sketching given characteristics*

*Analyzing derivative graphs*

*Analyzing velocity graphs*

*Velocity increasing/decreasing*

*Slowing down/speeding up*