

Tabular Data

Review: 4 Existence Theorems

1. IVT

Conditions:

Conclusion:

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2. EVT

Conditions:

Conclusion:

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3. MVT

Conditions:

Conclusion:

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4. Rolle's Theorem

Conditions:

Conclusion:

Use the table below with selected values of the twice differentiable function k . Read each explanation and decide whether you would apply IVT, EVT, MVT, or Rolle's. (Since f is differentiable, f is also continuous).

x	1	2	3	4	5	6	7
$f(x)$	5	2	-4	-1	3	2	0

a. Since $f(6) = 2$ and $f(7) = 0$ and since 1 is between 2 and 0, it follows by _____ that $f(c) = 1$ for some c .

Use the table below with selected values of the twice differentiable function k . Read each explanation and decide whether you would apply IVT, EVT, MVT, or Rolle's. (Since f is differentiable, f is also continuous).

x	1	2	3	4	5	6	7
$f(x)$	5	2	-4	-1	3	2	0

b. Since $\frac{f(3)-f(2)}{3-2} = -6$, it follows by _____ that $f'(c)=-6$ for some c in the interval $(2, 3)$.

Use the table below with selected values of the twice differentiable function k . Read each explanation and decide whether you would apply IVT, EVT, MVT, or Rolle's. (Since f is differentiable, f is also continuous).

x	1	2	3	4	5	6	7
$f(x)$	5	2	-4	-1	3	2	0

c. There must be a minimum value for f at some r in $[1, 7]$. Hence the _____ applies.

Use the table below with selected values of the twice differentiable function k . Read each explanation and decide whether you would apply IVT, EVT, MVT, or Rolle's. (Since f is differentiable, f is also continuous).

x	1	2	3	4	5	6	7
$f(x)$	5	2	-4	-1	3	2	0

d. There must be some value a in $(2, 6)$ for which $f'(a) = 0$ because $f(2) = f(6)$. Hence the _____ applies.

ex: Consider the differentiable function $v(t)$ with select values given in the table below.

t (min)	0	5	10	15	20	25	30
$v(t)$ (meters/min)	7	9.2	9.5	7	4.5	2.4	2.4

a) Estimate $a(7)$. Indicate units of measure.

t (min)	0	5	10	15	20	25	30
v(t) (meters/min)	7	9.2	9.5	7	4.5	2.4	2.4

b) Estimate $a(20)$. Indicate units of measure.

t (min)	0	5	10	15	20	25	30
v(t) (meters/min)	7	9.2	9.5	7	4.5	2.4	2.4

c) What is the smallest number of instances in which $v(t)=8$ on $(0, 30)$? Justify your answer.

t (min)	0	5	10	15	20	25	30
v(t) (meters/min)	7	9.2	9.5	7	4.5	2.4	2.4

d) What is the smallest number of instances in which $a(t)=0$ on $(0, 30)$? Justify your answer.

t (min)	0	5	10	15	20	25	30
v(t) (meters/min)	7	9.2	9.5	7	4.5	2.4	2.4

e) On the interval $(0, 20)$ must there be a time when $a(t) = -1/8$? Justify your answer.

Let $y(t)$ represent the population of the town of Sugar Mill over a 10-year period where y is a differentiable function of t . The table below shows the population recorded every two years.

$t(\text{years})$	0	2	4	6	8	10
$y(\text{people})$	2500	2912	3360	3815	4330	4875

- a. Approximate $y'(7)$ and explain the meaning of $y'(7)$ in terms of the population of Sugar Mill. Show the computations that lead to your conclusion. Include units of measure.

Let $y(t)$ represent the population of the town of Sugar Mill over a 10-year period where y is a differentiable function of t . The table below shows the population recorded every two years.

$t(\text{years})$	0	2	4	6	8	10
$y(\text{people})$	2500	2912	3360	3815	4330	4875

b. Find the average rate of change for $y(t)$ on the interval $(0, 10)$. Include units of measure.

Let $y(t)$ represent the population of the town of Sugar Mill over a 10-year period where y is a differentiable function of t . The table below shows the population recorded every two years.

$t(\text{years})$	0	2	4	6	8	10
$y(\text{people})$	2500	2912	3360	3815	4330	4875

c. Explain why there must be a time t in $(0, 10)$ such that $y(t) = 4000$.

In general, when given a differentiable function $f(x)$ and asked to show....

1. $f(x)=c$

Use:

Show:

In general, when given a differentiable function $f(x)$ and asked to show....

2. $f'(x)=c$

Use:

Show:

In general, when given a differentiable function $f(x)$ and asked to show....

3. $f'(x) = 0$

Use:

Show:

Existence Theorems - AP Style Questions

1.

Let $f(x) = x^3 - x - 1$. On the interval $[-1, 2]$ where does the instantaneous rate of change f equal the average rate of change of f on that interval?

- a) $-\frac{1}{2}$
- b) $-1, 1$
- c) 0
- d) 1
- e) $\frac{1}{2}$

*See printout.

2.

Which of the following functions below satisfy the conditions of the MVT?

I. $f(x) = \frac{1}{x+1}, [0,2]$ II. $f(x) = x^{1/3}, [0,1]$ III. $f(x) = |x|, [-1,1]$

- a) I only
- b) I and II only
- c) I and III only
- d) II only
- e) II and III only

3.

If f is continuous for $a \leq x \leq b$ and differentiable for $a < x < b$, which of the following could be false?

- (A) $f'(c) = \frac{f(b) - f(a)}{b - a}$ for some c such that $a < c < b$.
- (B) $f'(c) = 0$ for some c such that $a < c < b$.
- (C) f has a minimum value on $a \leq x \leq b$.
- (D) f has a maximum value on $a \leq x \leq b$.

4.

Let g be a continuous function on the closed interval $[0,1]$. Let $g(0) = 1$ and $g(1) = 0$. Which of the following is NOT necessarily true?

- (A) There exists a number h in $[0,1]$ such that $g(h) \geq g(x)$ for all x in $[0,1]$.
- (B) For all a and b in $[0,1]$, if $a = b$, then $g(a) = g(b)$.
- (C) There exists a number h in $[0,1]$ such that $g(h) = \frac{1}{2}$.
- (D) There exists a number h in $[0,1]$ such that $g(h) = \frac{3}{2}$.
- (E) For all h in the open interval $(0,1)$, $\lim_{x \rightarrow h} g(x) = g(h)$.

5.

x	0	1	2
$f(x)$	1	k	2

The function f is continuous on the closed interval $[0, 2]$ and has values that are given in the table above. The equation $f(x) = \frac{1}{2}$ must have at least two solutions in the interval $[0, 2]$ if $k =$

- (A) 0 (B) $\frac{1}{2}$ (C) 1 (D) 2 (E) 3