

$$19.) -3e^{2x} + 16 = 5$$

$$\ln e^{2x} = \ln \frac{11}{3}$$

$$2x = \ln \frac{11}{3}$$

$$x = \frac{\ln \frac{11}{3}}{2}$$

.6496

.650

$$52) \quad 2^{2x} - 12 \cdot 2^x + 32 = 0$$

$$a^2 - 12a + 32$$

$$(a-8)(a-4) = 0$$

$$a=8 \quad a=4$$

$$2^x = 8 \quad 2^x = 4$$

$$x=3$$

$$x=2$$

4.6 cont.



REVIEW: Condense.

$$\log(x - 2) + 2 \log x - 3 \log(x - 1)$$

REVIEW: Evaluate.

a) $\log_3\left(\frac{1}{9}\right)$

b) $\frac{\log 36}{\log 6}$

c) $\log_8(-8)$

d) $\log 0$

Domain of Logarithmic Functions

$$y = \log_b(f(x))$$

Domain: $f(x) > 0$

ex: State the domain in set notation.

a) $y = \log_2(x - 1)$

$$\{x \mid x > 1\}$$

$$x - 1 > 0$$

$$x > 1$$

ex: State the domain in set notation.

b) $y = 3 - \ln(-x)$

$$-x > 0$$

$$x < 0$$

$$\{x \mid x < 0\}$$

c) $y = \log_9(x^2 + 9)$

$$x^2 + 9 > 0$$

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$$\{x \mid x \in \mathbb{R}\}$$

Solving Logarithmic Equations

Two Types:

1. 1 Logarithm

$$\text{ex: } 2 - \log_2(x + 1) = 4$$

2. More than 1 Logarithm

$$\text{ex: } \log_3(x^2 - 3) = \log_3 2 + \log_3 x$$

3. Quadratic Form

When solving type 1 or 2, rewrite the equation with ONE TERM on each side of the equation.

ex: Solve.

$$a) \log_{36} x + \frac{1}{2} = 2$$

$$D: x > 0$$

$$\log_{36} x = \frac{3}{2}$$

Method 1:
take the base
of both sides

$$x = 36^{3/2}$$

$$216$$

Method 2:
rewrite as an
exponential

$$\log_{36} x = \frac{3}{2}$$

$$36^{3/2} = x$$

ex: Solve.

$$\text{b) } \log_{12}(x^2 - 4) = \log_{12}(3x)$$

$$x^2 - 4 = 3x$$

$$x^2 - 3x - 4 = 0$$

$$(x-4)(x+1) = 0$$

Check! $x=4$, ~~$x=-1$~~

ex: Solve.

$$c) \log_{31}(4x-5) - \log_{31}(2x-1) = 0$$

$$\log_{31}(4x-5) = \log_{31}(2x-1)$$

$$4x-5 = 2x-1$$

$$\boxed{x=2}$$

Check:

$$\log_{31} 3 - \log_{31} 3 = \log_{31} \left(\frac{3}{3}\right) = \log_{31} 1 = 0$$

$$\log_{31} \frac{4x-5}{2x-1} = 0$$

$$31^0 = \frac{4x-5}{2x-1}$$

$$1 = \frac{4x-5}{2x-1}$$

$$2x-1 = 4x-5$$
$$x=2$$

ex: Solve.

$$d) \log_2(4x-5) - \log_2(2x-1) = 3$$

Condense \rightarrow

$$\log_2 \frac{4x-5}{2x-1} = 3$$

$$\frac{4x-5}{2x-1} = 8$$

$$4x-5 = 16x-8$$

\emptyset

$$\cancel{x = \frac{1}{4}}$$

ex: Solve.

e) $\log 18 - \log 3x = \log 2$

$$\log_{10} \frac{18}{3x} = \log_{10} 2$$

$$\frac{18}{3x} = \frac{2}{1}$$

✓ $x = 3$

ex: Solve.

$$f) \frac{\ln(-x)}{2} + 4 = 5$$

$$e^{\ln(-x)} = e^2$$

$$-x = e^2$$

$$\checkmark \boxed{x = -e^2}$$

ex: Solve.

$$g) 2 \log x = \log 2 + \log 8$$

$$\log x^2 = \log 16$$

$$x^2 = 16$$

$$x = 4, \text{ } \cancel{x = -4}$$

ex: Solve.

$$h) \log_5 \sqrt{x-2} = 1$$

$$\frac{1}{2} \log_5 (x-2)^{\frac{1}{2}} = 1$$

$$\log_5 (x-2) = 2$$

$$x-2 = 25$$

$$\checkmark x = 27$$

$$\log_5 \sqrt{x-2} = 1$$

$$\sqrt{x-2} = 5$$

$$x-2 = 25$$

$$\checkmark x = 27$$

ex: Solve.

i) $3\log_x 49 - 2 = 4$

$$\log_x 49 = 2$$

$$49 = x^2$$

$$\boxed{7, -7 = x}$$

ex: Solve.

$$i) (\log_2 x)^2 - 4(\log_2 x) - 5 = 0$$

$$a = \log_2 x$$

$$a^2 - 4a - 5 = 0$$

$$(a-5)(a+1) = 0$$

$$a=5 \quad a=-1$$

$$\log_2 x = 5 \quad \log_2 x = -1$$

$x=32$	$\frac{1}{2}$
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Review

ex: Let

$$x = \log 7 \quad y = \log 14$$

Rewrite in terms of x and y .

$$\log 2$$

Review

ex: Solve.

$$9^{3x^2-6x} = 3^{x+5}$$

$$2^{3x} = 5^{x+1}$$

$$\frac{-\log 5}{\log 5 - \log 8}$$

$$x = 3.424$$

$$x = \frac{\log 5}{\log 8 - \log 5} = \frac{\log 5}{\log\left(\frac{8}{5}\right)}$$

$$2^{-3x} = 5^{x-1}$$

$$x = .436$$

$$x = \frac{\log 5}{\log 5 + 3 \log 2} = \frac{\log 5}{\log 40}$$

Review

ex: Solve.

$$6^{7x} = 2^{x+1}$$

$$\log 6^{3-6x} = \log(3^{x+5})$$

$$(3-6x)(\log 6) = (x+5)(\log 3)$$

$$\boxed{-.00994}$$

$$3(\log 6) - 6x(\log 6) = x(\log 3) + 5(\log 3)$$

$$3(\log 6) - 5(\log 3) = 6x(\log 6) + x(\log 3)$$

$$3(\log 6) - 5(\log 3) = x(6(\log 6) + (\log 3))$$

$$\frac{3\log 6 - 5\log 3}{6\log 6 + \log 3} = x$$

$$X = \frac{3 \log 6 - 5 \log 3}{6 \log 6 + \log 3}$$

$$X = \frac{\log 216 - \log 243}{\log(6^6 \cdot 3)}$$

$$X = \frac{\log \frac{216}{243}}{\log(139968)} = -.00994$$

Review

ex: Expand.

$$\log_5 \sqrt{\frac{x-2}{25y^3x^7}}$$