

$$8.) (10x^2 - 9x + 5) \div (2x - 1)$$

$$5x - 2 + \frac{3}{2x-1}$$

$$\begin{array}{r} 2x-1 \overline{) 10x^2 - 9x + 5} \\ \underline{-(10x^2 - 5x)} \phantom{+ 5} \\ -4x + 5 \\ \underline{-(-4x + 2)} \\ 3 \end{array}$$

$$\begin{array}{r} \div \\ \times \\ - \end{array}$$

$$6.) (x^4 + 3x^3 - 4x - 11) \div (x+3)$$

$$\begin{array}{r|rrrrr}
 -3 & 1 & 3 & 0 & -4 & -11 \\
 & \downarrow & -3 & 0 & 0 & 12 \\
 \hline
 & 1 & 0 & 0 & -4 & 1
 \end{array}$$

$$x^3 - 4 + \frac{1}{x+3}$$

10.)

$$k^2 + \frac{8}{2k+7}$$

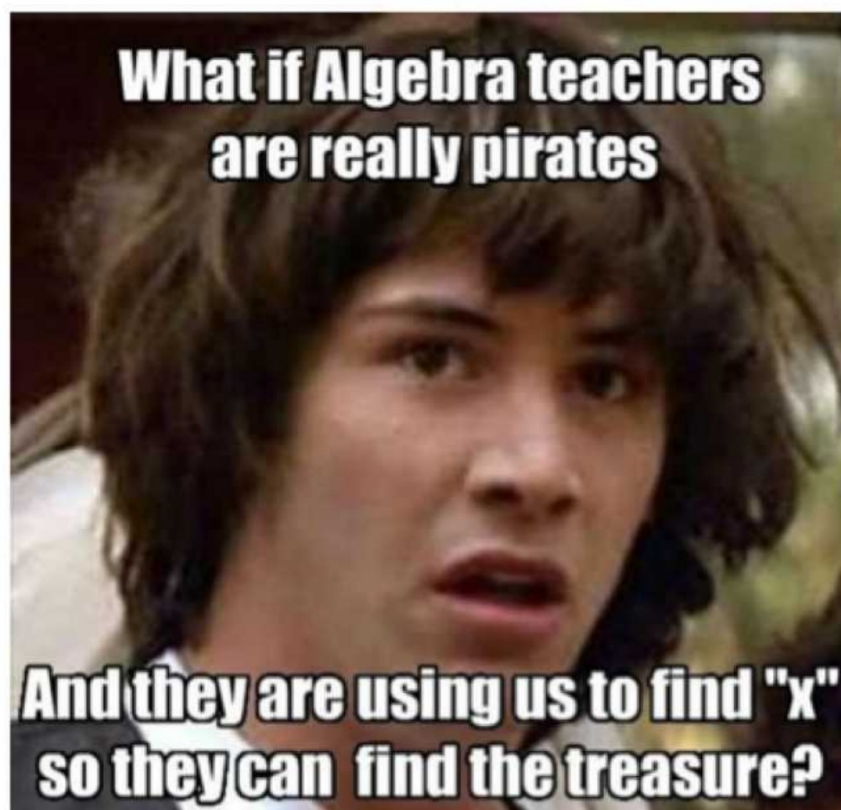
$$\begin{array}{r} 2k+7 \overline{) 2k^3 + 7k^2 + 0k + 8} \\ \underline{-(2k^3 + 7k^2)} \phantom{+ 0k + 8} \\ 0 + 0k \phantom{+ 8} \\ \underline{-(0 + 0)} \phantom{+ 8} \\ 8 \end{array}$$

$$\begin{array}{r} 18\frac{2}{3} \\ 3 \overline{) 47} \\ \underline{3} \phantom{00} \\ 17 \\ \underline{15} \\ 2 \end{array}$$

$$9.) (3a^3 - 8a^2 + 6a - 26) \div (a - 3)$$

$$\begin{array}{r}
 3a^2 + a + 9 + \frac{1}{a-3} \\
 a-3 \overline{) 3a^3 - 8a^2 + 6a - 26} \\
 \underline{-(3a^3 - 9a^2)} \\
 a^2 + 6a \\
 \underline{-(a^2 - 3a)} \\
 9a - 26 \\
 \underline{-(9a - 27)} \\
 1
 \end{array}$$

## A2 - Solving Polynomial Equations by Factoring



## Evaluating Polynomials

There are two ways to evaluate polynomial functions:

1. direct substitution
2. synthetic substitution

Direct Substitution (i.e. "PLUG IN")

ex: Find the indicated polynomial value using direct substitution.

a)  $f(x) = x^2 - 5x + 2$ ,  $f(13) = ?$

$$\begin{aligned} f(13) &= 13^2 - 5(13) + 2 \\ &= 169 - 65 + 2 \\ &= 169 - 63 = 106 \end{aligned}$$

$$f(13) = 106$$

Synthetic Substitution - substitution using a chart of coefficients

- \*Before using synthetic substitution,
  - the polynomial must be in standard form
  - consider if all terms are present

ex: Find the indicated value using synthetic substitution.

a)  $f(x) = x^2 - 5x + 2$ ,  $f(13) = ?$

13		1	-5	2
			13	104
		1	8	106

The result  $f(13) = 106$  is circled in purple, and a purple arrow points from the circled 106 in the table to the question mark in the equation.



ex: Find the indicated value using synthetic substitution.

b)  $g(x) = x^3 + 4x^2 - 1$ ,  $g(6) = ?$

$$\begin{array}{r|rrrr} 6 & 1 & 4 & 0 & -1 \\ & & 6 & 60 & 360 \\ \hline & 1 & 10 & 60 & 359 \end{array}$$

ex: Find the indicated value using synthetic substitution.

c)  $m(x) = 5x^4 + 2x$   ~~$2x$~~   $m(-2) = ?$  76

$$\begin{array}{r|rrrrr} -2 & 5 & 0 & 0 & 2 & 0 \\ & & -10 & 20 & -40 & 76 \\ \hline & 5 & -10 & 20 & -38 & \boxed{76} \end{array}$$

Theorem:

A polynomial equation with degree  $n$  has  $n$  solutions.

Vocabulary:

solutions/roots - answers to an equation

zeros - quantities that make a function equal to zero

ex: Solve by factoring.  
→ solutions - values of  $x$ .

a)  $x^2 - 8x + 15 = 0$

$$(x-5)(x-3) = 0$$

$$x-5=0 \quad x-3=0$$

$$\boxed{5, 3}$$

ex: Solve by factoring.

✓  
b)  $2x^4 + 7x^2 - 15 = 0$

$$(2x^2 - 3)(x^2 + 5) = 0$$

$$2x^2 - 3 = 0$$
$$\sqrt{x^2} = \sqrt{\frac{3}{2}}$$

$$x = \pm \sqrt{\frac{3}{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}}$$

$$x = \pm \frac{\sqrt{6}}{2}$$

$$x^2 + 5 = 0$$

$$\sqrt{x^2} = \sqrt{-5}$$

$$x = \pm i\sqrt{5}$$

ex: Solve by factoring.

c)  $24x^4 + 3x = 0$

ex: Solve by factoring.

$$d) \underbrace{x^3 - 5x^2} - \underbrace{9x + 45} = 0$$

$$x^2(x-5) - 9(x-5) = 0$$

$$(x^2 - 9)(x-5) = 0$$

$$(x+3)(x-3)(x-5) = 0$$

$$\boxed{-3, 3, 5}$$

ex: Solve by factoring.

e)  $x^4 + 2x^2 + 1 = 0$

$$(x^2 + 1)(x^2 + 1) = 0$$

$$\text{or } (x^2 + 1)^2 = 0$$

$$x^2 + 1 = 0$$

$$\sqrt{x^2} = \sqrt{-1}$$

$$x = \pm i$$

multiplicity of 2  
 $x = \pm i$



ex. Solve by factoring.

f)  $x^7 - 64x^5 = 0$

$$x^5(x^2 - 64) = 0$$

$$x^5(x-8)(x+8) = 0$$

$$x^5 = 0 \quad x-8 = 0 \quad x+8 = 0$$

$$x = 0$$

$$x = 8$$

$$x = -8$$

mult. of  
5

Solve.

$$x^2 (x-5)^3 (3x-1)^4 = 0$$

↓

$$x^2 = 0$$

$x = 0$   
mult. of  
2

↓

$$x-5=0$$

$x=5$   
mult. of  
3

↘

$$3x-1=0$$

$x = \frac{1}{3}$   
mult. of  
4