

IQR and Outliers

IQR: Inner Quartile Range

- **Sort the data: 4 5 6 8 9 11 11 11 11 19**
- **The “middle” is the median**
- **Median: 10**
- **Q_1 is midway between the smallest number and the median**
- **Q_1 : 6**
- **Q_3 is midway between the median and largest number**
- **Q_3 : 11**

5 number summary

- Minimum: 4
- Q_1 : 6
- Q_2 (median): 10
- Q_3 : 11
- Maximum: 19

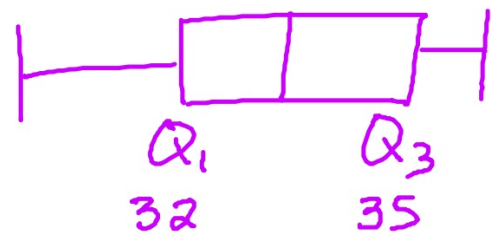
Is 19 an outlier?

IQR



- Inner-quartile range

$$Q3 - Q1$$



**This is the width of
your box**

Definition of an Outlier

- IQR: $Q_3 - Q_1$
- An outlier is any number that is below
- $Q_1 - 1.5 \times \text{IQR}$
- OR

$$Q_1 - 1.5(\text{IQR})$$

- An outlier is any number that is above
- $Q_3 + 1.5 \times \text{IQR}$

$$Q_3 + 1.5(\text{IQR})$$

Are there any values considered unusual?

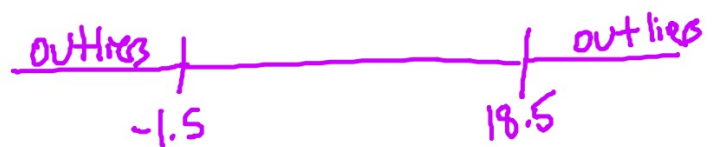
5 number summary

4, 6, 10, 11, 19

$$\begin{aligned} IQR &= Q_3 - Q_1 \\ &= 11 - 6 \\ &= 5 \end{aligned}$$

19 is an outlier

Lower	Upper
$Q_1 - 1.5(IQR)$	$Q_3 + 1.5(IQR)$
$6 - 1.5(5)$	$11 + 1.5(5)$
-1.5	18.5



4th grade test scores

Boys: 22, 17, 18, 29, 22, 22, 23, 24
23, 17, 21

Girls: 25, 20, 12, 19, 28, 24, 22, 21
25, 26, 25, 16, 27, 22

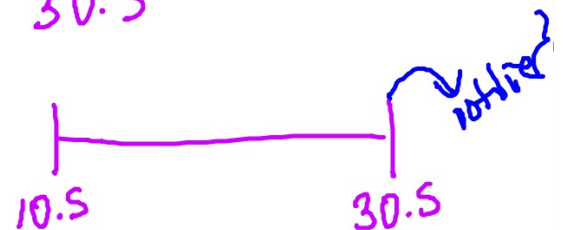
Are any of the scores for the boys considered an outlier?

22, 17, 18, 29, 22, 22, 23, 24, 23, 17, 21

$$Q_3 - Q_1$$
$$23 - 18$$
$$5$$

Lower	Upper
$Q_1 - 1.5(IQR)$	$Q_3 + 1.5(IQR)$
$18 - 1.5(5)$	$23 + 1.5(5)$
10.5	30.5

NO
Outliers



Are any of the scores for the girls considered an outlier?

25, 20, 12, 19, 28, 24, 22, 21, 25, 26, 25, 16, 27, 22

$$\begin{array}{r} Q_3 - Q_1 \\ 25 - 20 \\ 5 \end{array}$$

lower	upper
$Q_1 - 1.5(IQR)$	$Q_3 + 1.5(IQR)$
$20 - 1.5(5)$	$25 + 1.5(5)$
12.5 below	32.5 above

12 is an outlier