

Rectilinear Motion HW Answers

1. $\frac{dA}{dt} = \frac{2t+1}{2\sqrt{t}} + 2\sqrt{t} \text{ cm}^2/\text{s}$

2. $\frac{dV}{dt} = \frac{\pi}{2} \left(\frac{3t+2}{2\sqrt{t}} \right) \text{ in}^3/\text{s}$

3. $\frac{dC}{dx} = 100 \left(\frac{-400}{x^3} + \frac{30}{(x+30)^2} \right) \text{ dollars/order}$

- a. at $x=10, -38.13 \text{ dollars/order}$
- b. at $x=15, -10.37 \text{ dollars/order}$
- c. at $x=20, -3.80 \text{ dollars/order}$

As the order size increases the cost per order decreases.

4.

a. Average Velocity = $\frac{1}{2}$

b. $v(1) = 1, v(2) = \frac{1}{4}$

c. Speed at $x=1$ is 1, Speed at $x=2$ is $\frac{1}{4}$

5.

a. Average Velocity = $\frac{3}{\pi}$

b. $v(0) = 1, v\left(\frac{\pi}{6}\right) = \frac{\sqrt{3}}{2}$

c. Speed at $x=0$ is 1, Speed at $x=\frac{\pi}{6}$ is $\frac{\sqrt{3}}{2}$

6.

a. $v(t) = 20t^3 - 8t + 3$

b. $v(0) = 3$

c. $a(t) = 60t^2 - 8$

d. $a(0) = -8$

7.

a. $v(t) = \frac{-3}{5t^2}$

b. $v(2) = \frac{-3}{20}$

c. $a(t) = \frac{6}{5t^3}$

d. $a(2) = \frac{6}{40}$

8.

- a. Moving right on $(2, \infty)$ because $v(t) > 0$
- b. Moving Left on $(0, 2)$ because $v(t) < 0$

9.

- a. Moving right on $(0, 1)$ because $v(t) > 0$
- b. Moving Left on $(1, \infty)$ because $v(t) < 0$

10.

- a. $t = 1$ hr
- b. $s(1) = \frac{1}{12}$ miles

11.

- a. $t = \frac{1}{12}$ hr
- b. $s\left(\frac{1}{12}\right) = -3\sqrt{12} - \frac{\sqrt{12}}{12}$ miles

12.

- a. $v(t) = -2\pi t \sin\left(\frac{\pi}{2}t^2\right)$
- b. $a(t) = -2\pi^2 t^2 \cos\left(\frac{\pi}{2}t^2\right) - 2\pi \sin\left(\frac{\pi}{2}t^2\right)$
- c. Average Velocity = 0
- d. The ant is moving right on $(-1, 0)$ because $v(t) > 0$
- e. The particle changes directions at $t=0$ because $v(t)$ changes signs there.

13.

- a. $v(t) = 3\pi t \left(1 - \cos\left(\frac{3}{2}\pi t^2\right)\right)$
- b. $a(t) = 3\pi + 9\pi^2 t^2 \sin\left(\frac{3}{2}\pi t^2\right) - 3\pi \cos\left(\frac{3}{2}\pi t^2\right)$
- c. $t = 0, \sqrt{\frac{4}{3}}, \sqrt{\frac{8}{3}}$
- d. $x(0) = 0, x\left(\sqrt{\frac{4}{3}}\right) = 2\pi, x\left(\sqrt{\frac{8}{3}}\right) = 4\pi$