

## Rates of Change and Rectilinear Motion

Directions: Show all of your work on your OWN sheet of paper.

I.

1. The length of a rectangle is given by  $2t + 1$  and its height is  $\sqrt{t}$ , where  $t$  is time in seconds and the dimensions are in centimeters. Find the rate of change of the area with respect to time.
2. The radius of a right circular cylinder is given by  $\sqrt{t + 2}$  and its height is  $\frac{1}{2}\sqrt{t}$ , where  $t$  is time in seconds and the dimensions are in inches. Find the rate of change of the volume with respect to time.
3. The ordering and transportation cost  $C$  for the components used in manufacturing a product is given by  $C = 100\left(\frac{200}{x^2} + \frac{x}{x + 30}\right)$ ,  $x \geq 1$  where  $C$  is measured in dollars and  $x$  is the order size in hundreds. Find the rate of change of  $C$  when  $x=10$ ,  $x=15$ ,  $x=20$ . What do these rates of change imply about the ordering size?

II.

- a) Find the average rate of change of the function over the given interval.
- b) Find the instantaneous rate of change at the endpoints of the interval
- c) Find the speed at the endpoints of the interval.

4.  $s(t) = \frac{-1}{t}$ ,  $[1, 2]$

5.  $s(t) = \sin(t)$ ,  $[0, \frac{\pi}{6}]$

III.

A car is moving along I-75 according to the given position function, where  $s(t)$  is measured in meters, and  $t$  is measured in hours.

- a. Find an expression for the velocity function.
- b. Find the value of the velocity at the given time.
- c. Find an expression for the acceleration function.
- d. Find the value of the acceleration at the given time.

6.  $s(t) = 5t^4 - 4t^2 + 3t - 2$ ,  $t=0$

7.  $s(t) = \frac{3}{5t} - 2$ ,  $t=2$

IV.

A car is moving along I-595 according to the given position function, where  $s(t)$  is measured in miles, and  $t$  is measured in hours.

- a. Determine the values of  $t$  when the car is moving to the right.
- b. Determine the values of  $t$  when the car is moving to the left.

8.  $s(t) = 2t^3 + 9t^2 - 60t - 7$

9.  $s(t) = \frac{3t}{1 + t^2}$

V.

A car is moving along the Sawgrass Expressway according to the given position function, where  $s(t)$  is measured in miles, and  $t$  is measured in hours.

- a. Find the values of  $t$  for which the acceleration is zero.
- b. Find the position of the car at this time.

10.  $s(t) = \frac{t^4}{4} - \frac{t^3}{6} - t^2 + 1$

11.  $s(t) = -3\sqrt{t} - \frac{1}{12\sqrt{t}}, \quad t > 0$

VI.

12. An ant moves along the X-axis so that at time  $t$  its position is given by  $x(t) = 2\cos\left(\frac{\pi}{2}t^2\right)$ , for values of  $t$  on the interval  $[-1,1]$ .

- Find an expression for the velocity of the ant at any given time  $t$ .
- Find an expression for the acceleration at any given time  $t$ .
- Determine the average velocity of the ant over the given time interval.
- Determine the values of  $t$  for which the ant is moving to the right. Justify your answer.
- Determine the values of  $t$  for which the ant changes direction. Justify your answer.

13. A particle is moving along the X-axis so that its position for  $[0, 2]$  is given by

$$x(t) = \frac{3}{2}\pi t^2 - \sin\left(\frac{3}{2}\pi t^2\right).$$

- Find an expression for the velocity at any given time  $t$ .
- Find an expression for the acceleration at any given time  $t$ .
- Find the values for  $t$  for which the particle is at rest.
- Find the position of the particle at the time(s) found in part (c).

- Finish the AP problems we started in class.