

## Honors Calculus

### 6.2: Solving Differential Equations/Proportionality

#### Write and solve the differential equation that models the verbal statement

- 1) The rate of change of  $y$  with respect to  $t$  is directly proportional to the square root of  $t$ .
- 2) The rate of change of  $P$  with respect to  $t$  is inversely proportional to the square of  $t$ .
- 3) The rate of change of  $y$  with respect to  $t$  is proportional to  $y$ .
- 4) The rate of change of  $N$  with respect to  $t$  is inversely proportional to  $t$ .
- 5) The rate of change of  $y$  with respect to  $t$  is proportional to the square of  $t$ .

#### Write and solve the differential equation that models the verbal statement. Evaluate the solution at the specified value.

- 6) The rate of change of  $y$  is proportional to  $y$ . When  $x = 0$ ,  $y = 1/2$  and when  $x = 5$ ,  $y = 5$ . What is the value of  $y$  when  $x = 10$ ?
- 7) The rate of change of  $y$  is proportional to  $y$ . When  $x = 0$ ,  $y = 6$  and when  $x = 4$ ,  $y = 15$ . What is the value of  $y$  when  $x = 8$ ?

#### Find the exponential function, $y = a(b)^t$ that passes through the two given points.

8)  $(0, 3)$  and  $(4, 48)$

9)  $(1, 6)$  and  $(4, 16/9)$

#### Answers

1)  $y = \frac{2k}{3}t^{3/2} + C, y = kt^{3/2} + C$

2)  $P = \frac{-k}{t} + C, P = \frac{k}{t} + C$

3)  $y = Ce^{kt}$

4)  $N = k \ln|t| + C$

5)  $y = \frac{k}{3}t^3 + C, y = kt^3 + C$

6) 50

7)  $75/2$

8)  $y = 3(2)^t$

9)  $y = 9\left(\frac{2}{3}\right)^t$

