

Calculus**5.3: Derivative of inverse Functions**

Name _____

Period _____ Date _____

- If $f(x) = x^5 + x^3 + 2x - 2$, find $(f^{-1})'(2)$
- If $f(x) = \frac{1}{2}x^3 + \frac{1}{2}$, find $(f^{-1})'(0)$.
- If $f(x) = \frac{1}{4}x^3 + x - 1$, find $(f^{-1})'(3)$
- If $f(x) = x^3 - 3x^2 + 8x + 5$ and $g(x) = f^{-1}(x)$, find $g'(5)$
- If $f(x) = 2x^3 - 3x$, ($x \geq 0$), and $h(x)$ is the inverse function of $f(x)$, find $h'(-1)$.
- Given $f(3) = 15$, $f'(3) = -8$, $f(6) = 3$, and $f'(6) = -2$. If f and g are inverses, find $g'(3)$.
- Let $g(t) = 5t^2 - 10t + 4$ for $t \geq 1$. Find the value of $(g^{-1})'(4)$.
- Given $g(x) = \sin x$ on $\left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$. If f and g are inverses, find $f'\left(-\frac{1}{2}\right)$
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Selected values of a strictly monotonic function $g(x)$ and its derivative $g'(x)$ are shown on the table below.

x	-3	-1	1	4
$g(x)$	5	1	0	-3
$g'(x)$	-4	$-\frac{1}{5}$	$-\frac{1}{6}$	-2

- Find $(g^{-1})'(1)$
- Find $(g^{-1})'(-3)$

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Selected values of a strictly monotonic function $h(x)$ and its derivative $h'(x)$ are shown on the table below.

x	-1	0	2	4
$h(x)$	-5	-1	4	7
$h'(x)$	3	$\frac{1}{2}$	$\frac{1}{6}$	5

Let $f(x)$ be a function such that $f(x) = h^{-1}(x)$.

- Find $f'(-1)$
- Find $f'(4)$

Answers

1 $1/10$

2 $2/3$

3 $1/4$

4 $1/8$

5 $1/3$

6 $-1/2$

7 $1/10$

8 $2/\sqrt{3}$

9a -5

9b $-1/2$

10a 2

10b 6