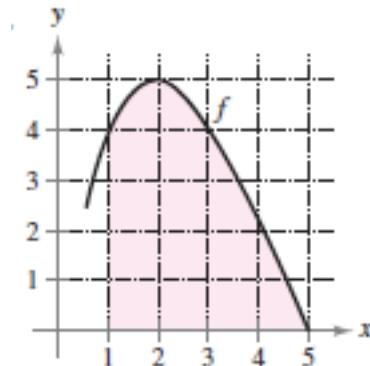


Honors Calculus: Area

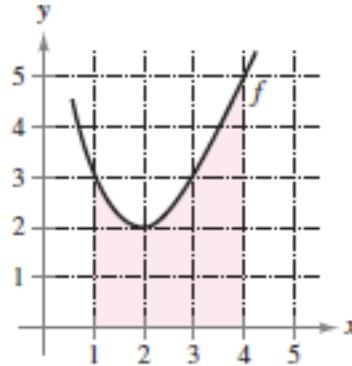
Estimate the area of the shaded region by using rectangles of equal width by utilizing:

- (a) Left Sum
- (b) Right Sum

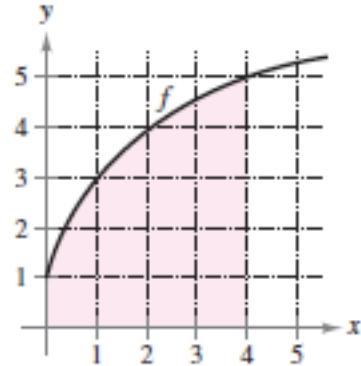
1)



2)



3)

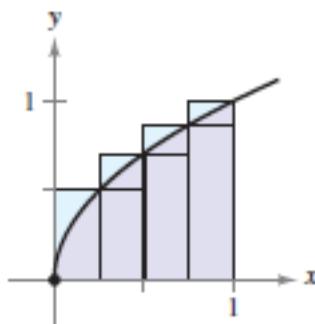


Approximate the area of the region bounded by the function and the x-axis over the indicated interval with subintervals of equal width by utilizing:

- (a) Left Sum
- (b) Right Sum

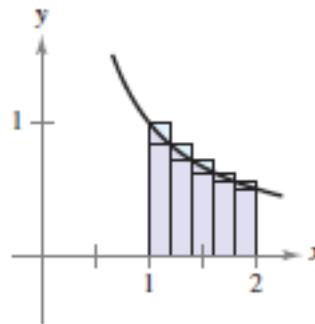
4)

$$y = \sqrt{x}$$



5)

$$y = \frac{1}{x}$$



Estimate the area of the region bounded by the graph of the function and the x-axis over the indicated interval with four subintervals by utilizing:

- (a) Left Sum
- (b) Right Sum
- (c) Midpoint Rule
- (d) Trapezoidal Rule

6) $f(x) = x^2$ [1, 5]

7) $f(x) = 2x^2 + 1$ [0, 4]

8) $f(x) = \sqrt{x} + 2$ [0, 2]

9) $f(x) = \tan x$ $\left[0, \frac{\pi}{4}\right]$

The tables list several values of an unknown continuous function $y = f(x)$. Estimate the area of the region bounded by the graph of the function and the x -axis over the interval on the table with the method indicated.

10) Trapezoidal Rule with 4 subintervals

x	0	8	14	22	24
f(x)	0	7	8	2	0

11) Right Sum with 5 subintervals

x	0	2	5	7	11	12
f(x)	5.7	4.0	2.0	1.2	0.6	0.5

12) Midpoint Sum with 4 subintervals

x	0	10	20	30	40	50	60	70	80
f(x)	5	14	22	29	35	40	44	47	49

13) Midpoint Sum with 4 subintervals

x	0	5	10	15	20	25	30	35	40
f(x)	7.0	9.2	9.5	7.0	4.5	2.4	2.4	4.3	7.3

14) Trapezoidal Rule

x	0	60	120	180	240	300	360
f(x)	24	30	28	30	26	24	26

15) Left Sum

x	2	3	5	8	13
f(x)	1	4	2	3	6

4.2 Area Worksheet Answers

1a 15
1b 11

2a 8
2b 10

3a 12.5
3b 16.5

4a .518
4b .768

5a .746
5b .646

6a 30
6b 54
6c 41
6d 42

7a 32
7b 64
7c 46
7d 48

8a 5.466
8b 6.173
8c 5.903
8d 5.819

9a .252
9b .448
9c .345
9d .350

10 115
11 19.3
12 2600
13 229
14 9780
15 30