

AP Calculus

5.3: Derivative of inverse Functions

Name_____

Period____ Date_____

1. If $f(x) = x^5 + x^3 + 2x - 2$, find $(f^{-1})'(2)$

2. If $f(x) = \frac{1}{2}x^3 + \frac{1}{2}$, find $(f^{-1})'(0)$.

3. If $f(x) = \frac{1}{4}x^3 + x - 1$, find $(f^{-1})'(3)$

4. If $f(x) = x^3 - 3x^2 + 8x + 5$, and $g(x) = f^{-1}(x)$, find $g'(5)$

5. If $f(x) = 2x^3 - 3x$, and $h(x)$ is the inverse function of $f(x)$, find $h'(-1)$, $x > 1/2$.

6. Given $f(3) = 15$, $f'(3) = -8$, $f(6) = 3$, and $f'(6) = -2$. If f and g are inverses, find $g'(3)$.

7. Suppose f is differentiable with the values shown in the table.

x	$f(x)$	$f'(x)$
0	2	1
1	3	2
2	5	3
3	10	4

- a. Write an equation of the tangent line to $f(x)$ at $x = 3$.
- b. Write an equation of the normal line to $f(x)$ at $x = 3$.
- c. Write an equation of the tangent line to $f^{-1}(x)$ at $x = 3$.
- d. Write an equation of the normal line to $f^{-1}(x)$ at $x = 3$.

Answers

- 1 $1/10$
 2 $2/3$
 3 $1/4$
 4 $1/8$
 5 $1/3$
 6 $-1/2$
 7a $y - 10 = 4(x - 3)$
 7b $y - 10 = -0.25(x - 3)$
 7c $y - 1 = \frac{1}{2}(x - 3)$
 7d $y - 1 = -2(x - 3)$