

4.6 Continued

Trigonometric Antiderivatives

$$\int \sin x \, dx =$$

$$\int \cos x \, dx =$$

$$\int \tan x \, dx =$$

$$\int \csc x \, dx =$$

$$\int \sec x \, dx =$$

$$\int \cot x \, dx =$$

ex: Integrate.

a) $\int \tan 5x \, dx$

ex: Integrate.

$$\text{b) } \int_{\pi/4}^{\pi/2} \sqrt{\csc^2 x - 1} \, dx$$

ex:

Evaluate $\int_0^{\frac{\pi}{4}} \frac{2e^{\tan x} + 5}{\cos^2 x} dx$

- (A) $2e+3$ (B) $2e$ (C) $2e-3$ (D) e (E) $e+5$

ex:

Evaluate $\int_e^{e^4} \frac{5}{x\sqrt{\ln x}} dx$

- (A) 6 (B) 7 (C) 8 (D) 9 (E) 10

FR 7

A particle starts at the point $(5, 0)$ at $t = 0$ and moves along the x -axis in such a way that at time $t > 0$ its velocity $v(t)$ is given by $v(t) = \frac{t}{1+t^2}$.

- (a) Determine the maximum velocity attained by the particle. Justify your answer.
- (b) Determine the position of the particle at $t = 6$.
- (c) Find the limiting value of the velocity as t increases without bound.

4.7 Inverse Trigonometry: Integration

Review:

$$\frac{d}{dx}[\sin^{-1} x] =$$

$$\frac{d}{dx}[\csc^{-1} x] =$$

$$\frac{d}{dx}[\cos^{-1} x] =$$

$$\frac{d}{dx}[\sec^{-1} x] =$$

$$\frac{d}{dx}[\tan^{-1} x] =$$

$$\frac{d}{dx}[\cot^{-1} x] =$$

THEOREM 4.20 Integrals Involving Inverse Trigonometric Functions

Let u be a differentiable function of x , and let $a > 0$.

1. $\int \frac{du}{\sqrt{a^2 - u^2}} =$

2. $\int \frac{du}{a^2 + u^2} =$

3. $\int \frac{du}{u\sqrt{u^2 - a^2}} =$

ex: Integrate.

a) $\int \frac{dx}{1+9x^2}$

ex: Integrate.

$$\text{b) } \int \frac{dx}{x\sqrt{4x^2 - 9}}$$

ex: Integrate.

$$c) \int \frac{\sin x dx}{\sqrt{25 - \cos^2 x}}$$

ex: Integrate.

$$d) \int \frac{7dx}{16+x^2}$$

ex: Integrate.

e) $\int \frac{x dx}{\sqrt{25 - x^2}}$

ex: Integrate.

$$g) \int \frac{e^{2x} dx}{1+e^{2x}}$$

ex: Integrate.

$$h) \int \frac{\sin x dx}{1 + \cos^2 x}$$

ex: Integrate.

$$k) \int \frac{\arccos x dx}{\sqrt{1-x^2}}$$

ex: Integrate.

★ 1) $\int \frac{dx}{x^2 - 2x + 2}$

ex: Integrate.

$$n) \int \frac{dx}{\sqrt{-x^2 - 4x}}$$

ex: Integrate.

$$o) \int \frac{dx}{x^2 + 4x + 13}$$

ex: Integrate.

★ p) $\int \frac{x+5}{\sqrt{9-x^2}} dx$

ex: Integrate.

★ q) $\int \frac{x+1}{x^2+9} dx$

ex: Integrate.

★
★ s) $\int \frac{2x-3}{\sqrt{4x-x^2}} dx$

ex: Integrate.

★ t) $\int \frac{x^3}{1+x^2} dx$