

## Chapter 8 Review

I. Vocabulary – Know the definition of each vocabulary word below.

- a. Parabola
- b. Circle
- c. Ellipse
- d. Hyperbola
- e. Latus rectum
- f. Major axis
- g. Minor axis
- h. Transverse axis
- i. Conjugate axis

II. Identify the conic and sketch its graph. Identify all that is applicable: center, radius, focus/foci, vertex/vertices, directrix, asymptotes, and axis of symmetry.

a.  $4x^2 + 16y^2 - 8x + 96y + 84 = 0$

b.  $y^2 + 6y + 2x + 11 = 0$

c.  $x^2 - 12x + 84 = -y^2 + 16y$

d.  $y^2 - 4x^2 + 8y + 16x - 4 = 0$

e.  $2x^2 + 6x + y^2 = \frac{1}{2}$

f.  $16y = 4x^2 - 8x$

III. Write an equation of the conic section in standard form with the given characteristics.

a. The circle passes through the origin and has its center at  $(-\sqrt{13}, 5)$ .

b. The ellipse that has endpoints of the major axis are at  $(2, 12)$  and  $(2, -4)$ . The endpoints of the minor axis are at  $(4, 4)$  and  $(0, 4)$ .

c. The parabola with vertex  $(-1, -2)$ , latus rectum length 12 and opens down.

d. The parabola with directrix  $x = 4$  and lower endpoint of the latus rectum at  $(8, 1)$ .

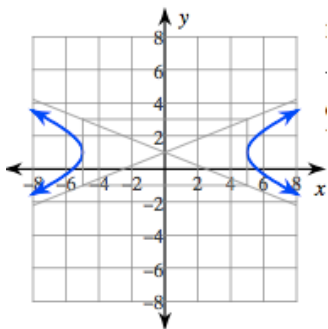
e. The hyperbola with center  $(3, 3)$ , vertex  $(1, 3)$  and focus  $(-1, 3)$ .

f. The hyperbola with center  $(0, 0)$  with vertices  $(0, 3)$  and  $(0, -3)$ ; asymptotes  $y = \pm x$

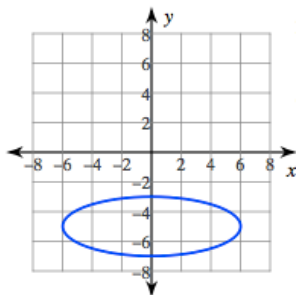
g. The ellipse with center  $(3, -4)$ ; major axis length 8 and parallel to the x-axis; minor axis length 2

IV. Write the equation for each of the conics in standard form.

a.



b.



V. Find all points of intersection.

<p>a.  <math>x^2 + y^2 = 100</math>  <math>y - x = 2</math></p>	<p>b.  <math>x^2 + y^2 = 34</math>  <math>x^2 - 2y^2 = 7</math></p>	<p>c.  <math>3x^2 + 4x - y = 7</math>  <math>2x - y = -1</math></p>	<p>d.  <math>x^2 + y^2 = 9</math>  <math>y = x^2 + 3</math></p>
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VI.

<p>a. Sketch. Find all points of intersection.  <math>x^2 + y^2 = 25</math>  <math>y^2 = x + 5</math></p>	<p>b. Find the distance between the point (8,3) and the focus for  <math>x^2 - 4x - 4y = 0</math></p>	<p>c. Write the equation of a circle whose endpoints of a diameter are (5, 1) and (3, -2)</p>
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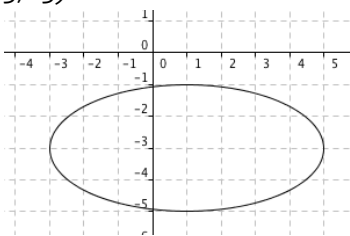
Answers

I.

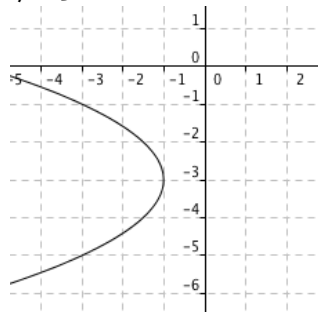
Refer to your textbook for the formal definitions.

II.

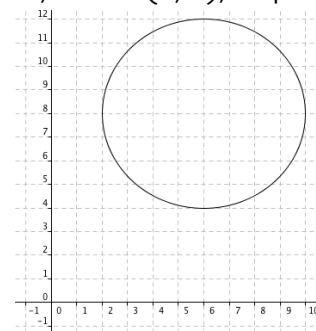
a. ellipse, center (1, -3), foci  $(1 \pm 2\sqrt{3}, -3)$ , vertices (5, -3) & (-3, -3)



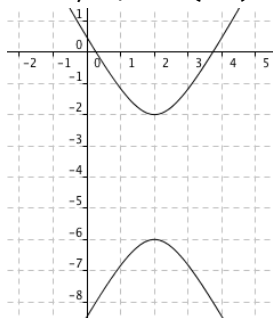
b. parabola, vertex (-1, -3), focus  $(-3/2, -3)$ , directrix  $x = -1/2$ , AOS:  $y = -3$



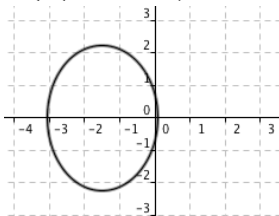
c. circle, center (6, 8), r=4



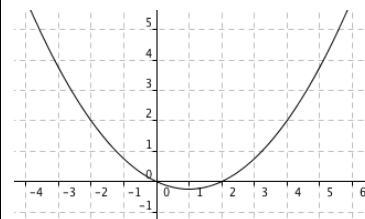
d. hyperbola, center (2, -4), vertices (2, -2) & (2, -6), foci  $(2, -4 \pm \sqrt{5})$ , asymptotes  $y + 4 = \pm 2(x - 2)$



e. ellipse, center  $(-3/2, 0)$ , foci  $(-3/2, \pm \frac{\sqrt{10}}{2})$ , vertices  $(-3/2, \pm \sqrt{5})$



f. parabola, vertex  $(1, -1/4)$ , focus  $(1, 3/4)$ , directrix  $y = -5/4$ , AOS:  $x = 1$



III.

a. $(x + \sqrt{13})^2 + (y - 5)^2 = 38$	b. $\frac{(x - 2)^2}{4} + \frac{(y - 4)^2}{64} = 1$	c. $(x + 1)^2 = -12(y + 2)$
d. $(y - 5)^2 = 8(x - 6)$	e. $\frac{(x - 3)^2}{4} - \frac{(y - 3)^2}{12} = 1$	
f. $\frac{y^2}{9} - \frac{x^2}{9} = 1$	g. $\frac{(x - 3)^2}{16} + \frac{(y + 4)^2}{1} = 1$	

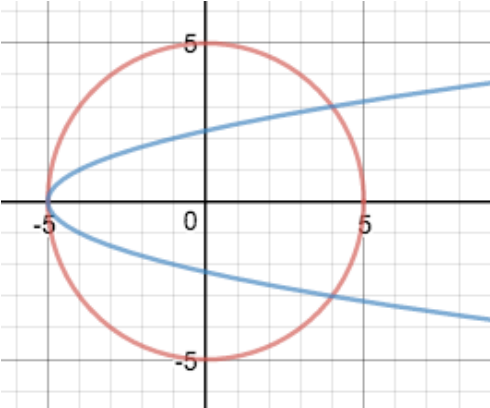
IV.

a. $\frac{x^2}{25} - \frac{(y - 1)^2}{4} = 1$	b. $\frac{x^2}{36} + \frac{(y + 5)^2}{4} = 1$
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V.

a. $(-8, -6)$ and $(6, 8)$	b. $(5, 3), (5, -3), (-5, 3), (-5, -3)$	c. $(4/3, 11/3)$ and $(-2, -3)$	d. $(0, 3)$
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VI.

a.  $(-5, 0), (4, 3), (4, -3)$	b. $3\sqrt{5}$	c. $(x - 4)^2 + \left(x + \frac{1}{2}\right)^2 = \frac{13}{4}$
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