

$$10.) \quad 10^{3x-10} = \left(\frac{1}{100}\right)^{6x-1}$$
$$10^{3x-10} = 10^{-2(6x-1)}$$
$$3x-10 = -12x+2$$
$$15x = 12$$
$$x = \frac{4}{5}$$

$$8.) \quad 3^{3x-7} = 3^{4(12-3x)}$$

$$3x-7 = 48-12x$$

$$\frac{11}{3}$$

$$5.) \quad 2^{3(x-1)} = 2^{5(3x-2)}$$

$$3x - 3 = 15x - 10$$

$$7 = 12x$$

$$\frac{7}{12} = x$$

$$\text{II.) } (5^2)^{10x+8} = 5^{-3(4-2x)}$$

$$20x + 16 = -12 + 6x$$

$$14x = -28$$

$$x = -2$$

4.6 Solving Exponential & Logarithmic Equations



HW:

3 Types of Exponential Equations:

- ✓ 1. $a^x = b$, where a and b are integral powers of the same number

$$\text{ex: } 27^x = 9$$

- ✓ 2. $a^x = b$, where a and b are NOT integral powers of the same number

$$\text{ex: } 3^x = 5$$

3. quadratic form

$$\text{ex: } 3^{2x} + 3^x - 6 = 0$$

REVIEW:

ex: Solve.

$$27^{3x-7} = 81^{12-3x}$$

Type 2

ex: Solve.

a) $3^x = 5$

$$\log_3 5 = x$$

$$\frac{\log 5}{\log 3} = x$$

$$1.465 = x$$

$$3^x = 5$$

$$\log 3^x = \log 5$$

$$\frac{x \log 3}{\log 3} = \frac{\log 5}{\log 3}$$

$$x =$$

ex: Solve.

b) $e^{x+1} = 10$

$$\ln e^{x+1} = \ln 10$$
$$(x+1) = \ln 10$$

$$x = -1 + \ln 10$$

$$x = 1.303$$

ex: Solve.

c) $3 \cdot 4^{x-7} + 6 = 54$

$$4^{x-7} = 16$$

$$4^{x-7} = 4^2$$

$$x-7 = 2$$

$$x = 9$$

ex: Solve.

d) $2 \cdot 10^{x-3} - 3 = 37$

$$\log 10^{x-3} = \log 20$$

$$(x-3) = \log 20$$

$$x = 3 + \log 20$$

$$= 4.301$$

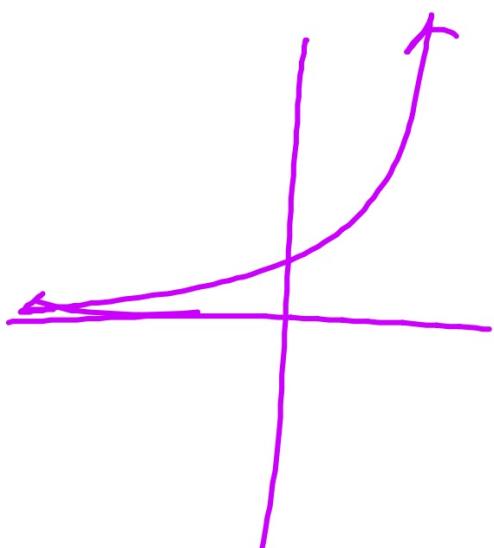
ex: Solve.

e) $2 - 5^{x-2} = 3$

$$-5^{x-2} = 1$$

$$5^{x-2} = -1$$

\emptyset



ex: Solve.

f) $5^{x-1} = 3^{x+2}$

$$\log 5^{x-1} = \log 3^{x+2}$$

$$(x-1)\log 5 = (x+2)\log 3 \quad \leftarrow \text{log property}$$

$$(x-1)\log 5 = x\log 3 + 2\log 3 \quad \leftarrow \text{distributive}$$

$$x\log 5 - \log 5 = x\log 3 + 2\log 3 \quad \leftarrow \begin{matrix} \text{get } x \text{ s on} \\ \text{same side} \\ (+ \text{ constants}) \end{matrix}$$

$$\frac{x(\log 5 - \log 3)}{\log 5 - \log 3} = \frac{\log 5 + 2\log 3}{\log 5 - \log 3} \quad \leftarrow \begin{matrix} \text{factor out } x \\ \text{divide} \end{matrix}$$

$$x = \frac{\log 5 + 2\log 3}{\log 5 - \log 3} = \frac{\log 5 + \log 9}{\log(5/3)} = \frac{\log 45}{\log(5/3)}$$

ex: Solve.

$$g) 5^{2x-7} = 4^{x+1}$$
$$\log 5^{\cancel{2x}-7} = \log 4^{x+1}$$

$$(2x-7)\log 5 = (x+1)\log 4 \quad x = \frac{\log 312500}{\log 25/4}$$

$$2x\log 5 - 7\log 5 = x\log 4 + \log 4$$

$$2x\log 5 - x\log 4 = \log 4 + 7\log 5$$

$$x = \frac{\log 4 + 7\log 5}{\log 25 - \log 4} = 6.904$$

Type 3

ex: Solve.

$$\text{J) } 2^{2x} - 5 \cdot 2^x - 24 = 0$$
$$(2^x - 8)(2^x + 3) = 0$$
$$2^x - 8 = 0 \quad 2^x + 3 = 0$$
$$2^x = 8$$
$$2^x = -3$$
$$\boxed{x = 3}$$

ex: Solve.

k) $4^{2x} - 7 \cdot 4^x + 12 = 0$

$$(4^x - 3)(4^x - 4) = 0$$

$$4^x = 3 \quad 4^x = 4$$

$$\log_4 3 = x$$

$$x = 1$$

$$x = \frac{\log 3}{\log 4}$$

MIXED PRACTICE

ex: Solve.

a) $5 \cdot 2^x - 3 = 157$

b) ~~$2 \cdot 3^{2x} - 4 \cdot 3^x - 12 = 0$~~ $3^{2x} - 4 \cdot 3^x - 12 = 0$

c) $8^{x+1} = 4^{x-3}$

d.) $\frac{81^{3-x}}{3^{x+1}} = \left(\frac{1}{3}\right)^{6x-5}$

e) $7^{x+10} = 3^{2x-1}$

$3^{4(3-x)} = 3^{1(6x-5)}$

$4(3-x) - (x+1) = -1(6x-5)$

$$3.) \log_2 \left(\frac{x^4}{32(y^8+2)} \right)^{1/2}$$

$$\frac{1}{2} \left[4\log_2 x - \log_2 32 - \log_2 (y^8 + 2) \right]$$

$$\frac{1}{2} \log_5(25x^2y^5)$$

$$\frac{1}{2} \left[(\cancel{\log_5 25}) + 2\log_5 \cancel{x} + 5\log_5 \cancel{y} \right]$$

$$\begin{aligned}\log \frac{1}{75} &= \log 1 - \log 75 \\&= 0 - (\log 5 + \log 5 + \log 3) \\&= 0 - (x + x + y) \\&\quad \boxed{-2x-y}\end{aligned}$$

$\log_6 36$

2