

$$\sqrt[4]{125}$$

$$\begin{array}{c} 16 \\ 81 \\ \hline 256 \end{array}$$

$$\begin{array}{c} 3^4 \\ 4^4 \end{array}$$

$$\frac{1}{(4^3)^{2/3}}$$

$$\frac{1}{16}$$

$$3 < \sqrt[4]{125} < 4$$

$$\textcircled{1} \quad \sqrt{x^5} = x^{5/2}$$

$$\textcircled{2} \quad 64^{-2/3} = \frac{1}{16}$$

$$\begin{array}{r} 128 \\ (2^7) \\ 32 \end{array} \begin{array}{r} ^{5|7} \\ ^{5|7} \end{array}$$

### 3.2: Operations with rational exponents

Skip #9 and #10

Simplify

$$a) \sqrt[3]{64} = 4$$

$$b) \sqrt[5]{-243} = -3$$

$$c) \sqrt[4]{81} = \text{nonreal}$$

$$d) \sqrt{18} = 3\sqrt{2}$$

$$e) \sqrt[3]{24}$$

$$\frac{\sqrt[3]{8} \cdot \sqrt[3]{3}}{2 \sqrt[3]{3}} \quad \left| \begin{array}{l} \sqrt[3]{2 \cdot 2 \cdot 2 \cdot 3} \\ \hline 2 \sqrt[3]{3} \end{array} \right.$$

$$f.) \sqrt[5]{-96} = \sqrt[5]{-32} \cdot \sqrt[5]{3} = -2\sqrt[5]{3}$$
$$- \sqrt[5]{2 \cdot 2 \cdot 2 \cdot 2 \cdot 3} = -2\sqrt[5]{3}$$

$$g.) \sqrt[5]{128} = \sqrt[5]{32} \cdot \sqrt[5]{4} = 2\sqrt[5]{4}$$

$$h.) \sqrt[3]{81} = \sqrt[3]{27} \cdot \sqrt[3]{3} = 3\sqrt[3]{3}$$

## Operations:

Adding/subtracting - you must have like radicals  
(which means same index and radicand)  $2\sqrt[4]{5} + 3\sqrt[4]{5}$

Multiplication/Division - the index must be the same

$$\sqrt[3]{12} \cdot \sqrt[3]{4}$$

Perform the indicated operation

$$a) \sqrt[4]{10} + 7\sqrt[4]{10} = 8\sqrt[4]{10}$$

$$b) \sqrt[3]{12} \cdot \sqrt[3]{18} = \sqrt[3]{2 \cdot 2 \cdot 3 \cdot 3 \cdot 3 \cdot 2} = 3 \cdot 2 = 6$$

$$c) \sqrt[3]{54} - \sqrt[3]{2} =$$

$$\sqrt[3]{27} \cdot \sqrt[3]{2} - \sqrt[3]{2}$$

$$3\sqrt[3]{2} - \sqrt[3]{2}$$

$$2\sqrt[3]{2}$$

$$d.) \frac{\sqrt[3]{250}}{\sqrt[3]{2}} = \sqrt[3]{125} = 5$$

$$e.) \sqrt{\frac{7}{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}} = \frac{\sqrt{14}}{2}$$

$$f.) \sqrt[3]{\frac{11}{2}} = \frac{\sqrt[3]{11}}{\sqrt[3]{2}} \cdot \left( \frac{\sqrt[3]{4}}{\sqrt[3]{4}} \right) = \frac{\sqrt[3]{44}}{\sqrt[3]{8}} = \frac{\sqrt[3]{44}}{2}$$

$$g.) \frac{\sqrt[4]{5}}{\sqrt[4]{10}} = \frac{1}{\sqrt[4]{2}} \cdot \frac{\sqrt[4]{8}}{\sqrt[4]{8}} = \frac{\sqrt[4]{8}}{\sqrt[4]{16}} = \frac{\sqrt[4]{8}}{2}$$

$$h.) \frac{2}{\sqrt[4]{9}} = \frac{2}{\sqrt[4]{3^2}} \left( \frac{\sqrt[4]{3^2}}{\sqrt[4]{3^2}} \right) = \frac{2\sqrt[4]{9}}{3}$$

$$i.) \begin{array}{l} 16^{1/4} \cdot 16^{3/2} \\ 16^{\frac{1}{4} + \frac{3}{2}} \\ 16^{7/4} \\ (2^4)^{7/4} \\ 128 \end{array} \quad \left| \quad \begin{array}{l} 16^{1/4} \cdot 16^{3/2} \\ (2^4)^{1/4} \cdot (4^2)^{3/2} \\ 2 \cdot 4^3 \\ 2 \cdot 64 \\ 128 \end{array} \right.$$

$$j) \left( 6^{\frac{1}{12}} \cdot 8^{\frac{1}{16}} \right)^2$$
$$\begin{matrix} 6^1 \cdot 8 \\ 6^1 \cdot 2 \\ 12 \end{matrix}$$

$$8^{\frac{1}{13}} = \sqrt[3]{8}$$

$$k) \left( 4^{\frac{5}{3}} \cdot 4^{\frac{3}{4}} \right)^{-\frac{1}{4}}$$
$$\begin{matrix} (4^8)^{-\frac{1}{4}} \\ 4^{-2} \\ \frac{1}{4^2} \\ \frac{1}{16} \end{matrix}$$

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$$1) \frac{3}{2^{1/3}} = \frac{3}{\sqrt[3]{2}} \cdot \frac{\sqrt[3]{4}}{\sqrt[3]{4}} = \frac{3\sqrt[3]{4}}{2} \quad \text{?} \\ \frac{3}{2^{1/3}} \cdot \left( \frac{2^{2/3}}{2^{2/3}} \right) = \frac{3 \cdot 2^{2/3}}{2^1} \quad \frac{3 \cdot \sqrt[3]{2^2}}{2}$$

$$\frac{1}{3} + \square = 1$$