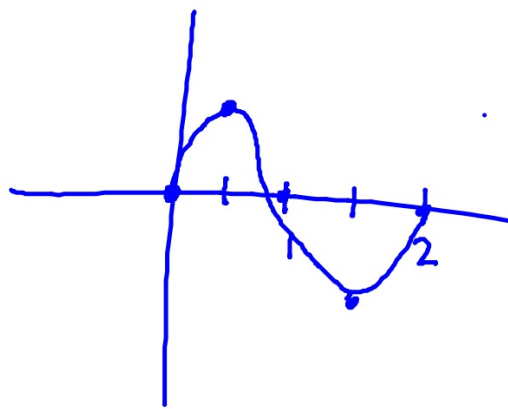


9.  $y = \sin \pi x$

Amp: 1

Period: 2

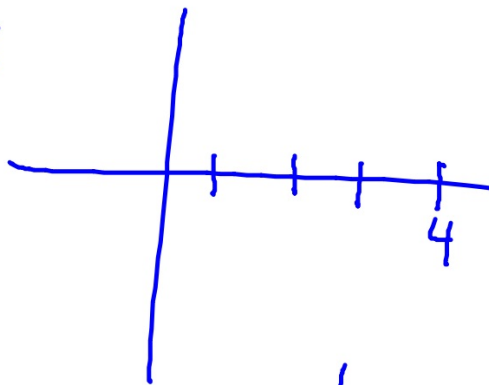
incr.  $\frac{2}{4} = \frac{1}{2}$



$$11. y = \sin \frac{\pi}{2} x$$

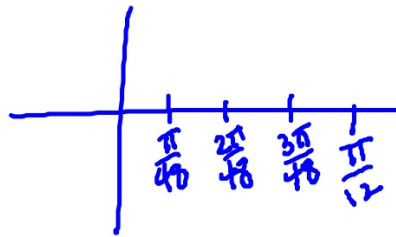
amp: 1

$$\text{period } \frac{2\pi}{\frac{\pi}{2}} = 4$$



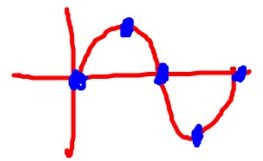
$$13.) y = \cos 24x$$

$$a = 1$$
$$\text{per: } \frac{2\pi}{24} = \frac{\pi}{12}$$



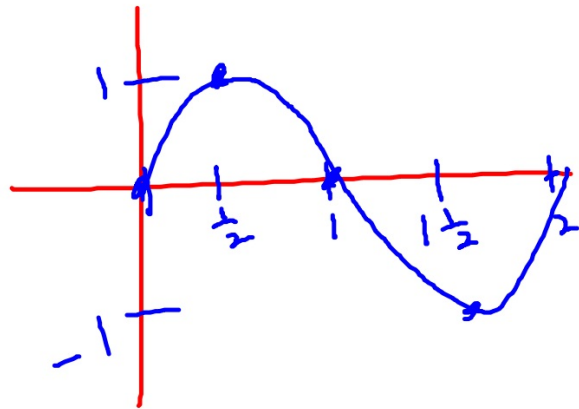
## 10.2 Transformations of $\sin x$ and $\cos x$

9.)  $y = \sin \pi x$



period:  $\frac{2\pi}{\pi}$   
2

incr:  $\frac{1}{2}$



## Transformations

$$y = 3\sin 2x - 1$$

$$y = a\sin b(x - c) + d \quad \text{or} \quad y = a\cos b(x - c) + d$$

a: Amplitude  $|a|$

b: This value determines the period of the function

$$\text{period} = 2\pi/b$$

c: phase shift (aka horizontal translation)

d: vertical shift

$$y = a \sin \underbrace{b(x + c)} + d$$

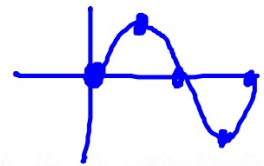
$$(bx + c)$$

How to  
find the  
phase shift

Horizontal translation  
Phase shift (PS)

$bx - c = 0$	$b(x + c) = 0$
$y = 2 \cos(2x - \pi) - 1$	$y = 3 \sin 2(x + 8)$
$2x - \pi = 0$	$2(x + 8) = 0$
$x = \frac{\pi}{2}$	$x = -8$
right $\frac{\pi}{2}$	8 left

#1  $y = \sin\left(x + \frac{\pi}{2}\right) + 1$



Amplitude 1

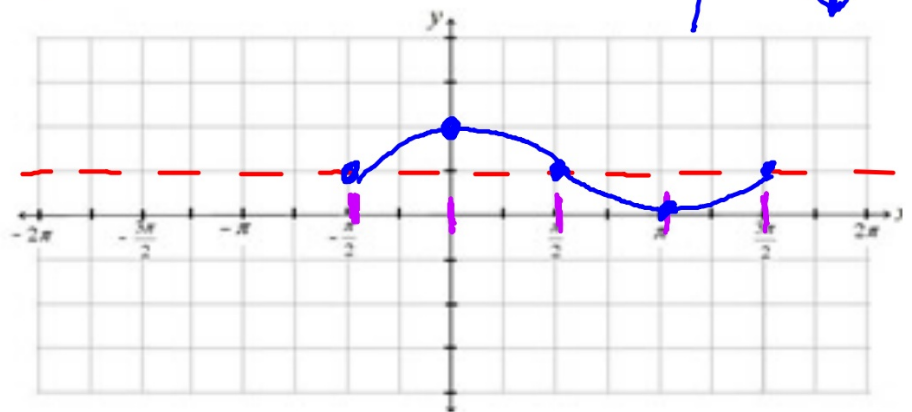
period  $2\pi$

Increments  $\frac{\pi}{2}$

vertical shift up 1

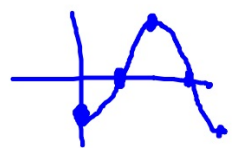
phase shift  $x + \frac{\pi}{2} = 0$

left  $\frac{\pi}{2}$   $x = -\pi/2$



Domain  $(-\infty, \infty)$   
Range  $[0, 2]$

#2  $y = -2 \cos(4x - \pi) + 1$



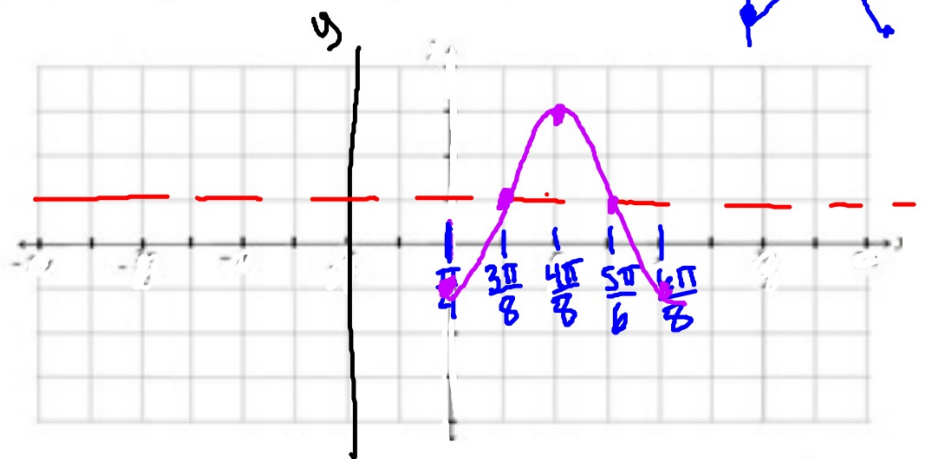
Amplitude 2

period  $\frac{2\pi}{b} = \frac{\pi}{2}$

Increments  $\frac{\pi}{8}$

vertical shift up 1

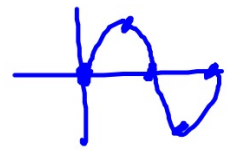
phase shift right  $\frac{\pi}{4}$



Domain  $(-\infty, \infty)$   
Range  $[-1, 3]$



#3  $y = 3 \sin(2x + \pi)$



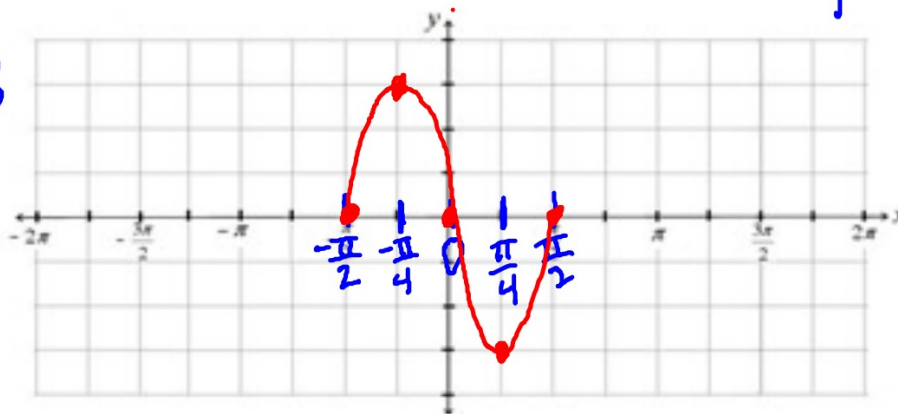
Amplitude 3

period  $\pi$

Increments  $\pi/4$

vertical shift n/a

phase shift left  $\frac{\pi}{2}$



$$-\frac{\pi}{2} + \frac{\pi}{4}$$

$$-\frac{\pi}{4}$$

Domain  $\{x | x \in \mathbb{R}\}$   
 Range  $\{y | -3 \leq y \leq 3\}$