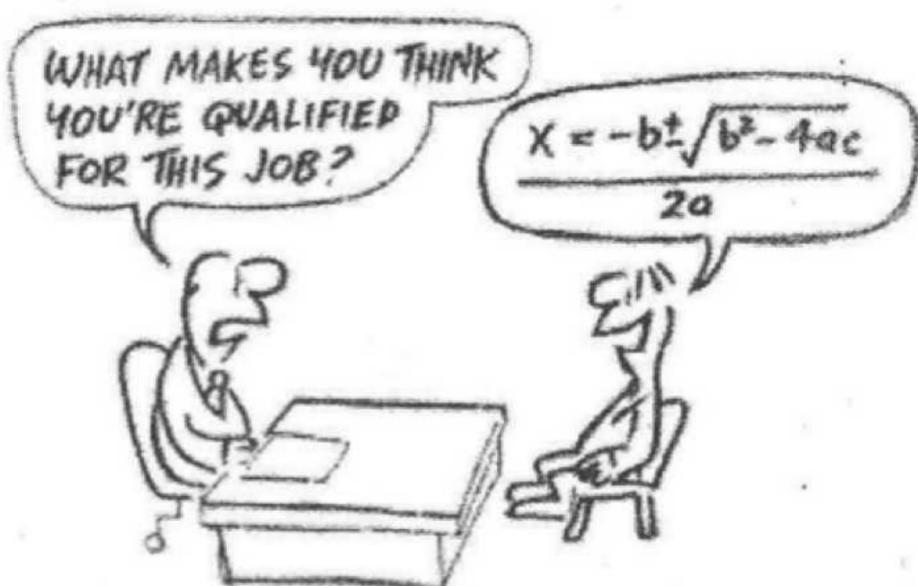


## 1.7 Solving Quadratic Equations Using CTS

## 1.8 Quadratic Formula



## Solving Quadratics By CTS

\*Use CTS to solve a quadratic equation when...

"b" value is even, and  
the equation  
is not  
factorable

ex: Solve.

a)  $x^2 - 4x - 10 = 0$

$$\left(\frac{-4}{2}\right)^2 = 4$$

$$(x^2 - 4x + 4) - 10 = 0$$

$$\sqrt{(x-2)^2} = \sqrt{14}$$

$$|x-2| = \sqrt{14}$$

$$x-2 = \pm \sqrt{14}$$

$$x = 2 \pm \sqrt{14}$$

$$\text{b) } x^2 - 14x + 103 = 0$$

$$\begin{aligned} & \overbrace{x^2 - 14x + \underline{49} - \underline{49}}^{(x-7)^2} + 103 = 0 \\ & \sqrt{(x-7)^2} = \sqrt{-54} \quad 3 \pm 5 \\ & |x-7| = 3i\sqrt{6} \quad 3+5 \quad 3-5 \\ & x-7 = \pm 3i\sqrt{6} \quad 8 \quad -2 \\ & x = 7 \pm 3i\sqrt{6} \end{aligned}$$

$$c) \underline{-2x^2 + 4x - 17 = 0}$$

$$\underline{-2(x^2 - 2x + 1) + 2} - 17 = 0$$

$$-2(x-1)^2 = 15$$

$$\sqrt{(x-1)^2} = \sqrt{\frac{-15}{-2} \cdot \frac{12}{12}}$$

$$|x-1| = \frac{i\sqrt{30}}{2}$$

$$x = 1 \pm \frac{i\sqrt{30}}{2}$$

$$d) 4x^2 + 12x + 1 = 0$$

$$4(x^2 + 3x)$$

$\uparrow$   
odd  
not friendly

## Solving Quadratics Using the Quadratic Formula

Let  $a, b, c \in R$  such that  $a \neq 0$ . The solutions of the quadratic equation  $ax^2 + bx + c = 0$  are:

Quadratic Formula:  $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

\*Use the Quadratic Formula to solve a quadratic equation when... other methods are not feasible

ex: Solve.

$$\frac{6 \pm 8\sqrt{3}}{2} = \frac{6}{2} \pm \frac{8\sqrt{3}}{2}$$
$$3 \pm 4\sqrt{3}$$

a)  $x^2 + 3x - 2 = 0$

$$x^2 + 3x - 2 = 0$$

$$a = 1$$

$$b = 3$$

$$c = -2$$

$$x = \frac{-3 \pm \sqrt{3^2 - 4(1)(-2)}}{2(1)}$$

$$= \frac{-3 \pm \sqrt{17}}{2} = \frac{-3}{2} \pm \frac{\sqrt{17}}{2}$$

$$b) -x^2 + 4x - 5 = 0$$

$$a = -1 \quad x = \frac{-4 \pm \sqrt{16 - 4(-1)(-5)}}{2(-1)}$$

$$b = 4$$

$$c = -5 \quad x = \frac{-4 \pm \sqrt{-4}}{-2}$$

$$= \frac{-4 \pm 2i}{-2} = \frac{-4}{-2} \pm \frac{2i}{-2}$$

$$2 \pm i$$

## Picking A Method

*look for square method*

*look for 'factorable'*

*CTS or quadratic formula*

ex: Determine which method is best to solve each quadratic equation. Do not repeat a method. DO NOT SOLVE.

a)

$$1. \ x^2 + 6x - 3 = 0$$

CTS

$$2. \ x^2 + 6x + 5 = 0$$

Factor

$$3. \ 2(x+1)^2 - 4 = 0$$

Sq. root

$$4. \ x^2 + 2x + 5 = 0$$

quad form

b)

$$1. \ 14x^2 - 21x = 0 \quad \text{factorable}$$

$$2. \ x^2 + 3x - 1 = 0 \quad \text{Quadratic form}$$

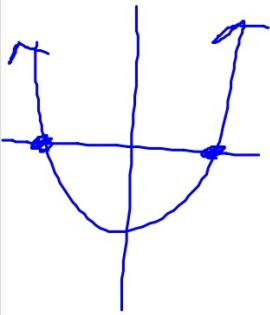
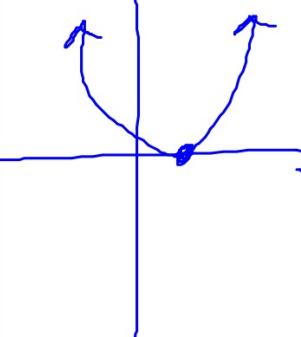
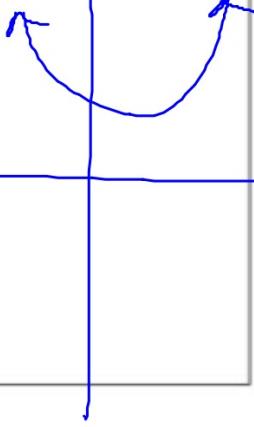
$$3. \ 2x^2 - 8x + 5 = 0 \quad \text{CTS}$$

$$4. \ x^2 - 80 = 0 \quad \text{Square root}$$

### The Discriminant:

- In the quadratic formula, the expression  $b^2 - 4ac$  is called the discriminant.
- The discriminant is used to determine the types of solutions for the quadratic.

## Using The Discriminant:

Value of discriminant	$D > 0$	$D = 0$	$D < 0$
Number of solutions	2	1	2
Type of solutions	real	real	imaginary
Graph of $y = ax^2 + bx + c$			

ex: Find the discriminant and give the number and type of solutions of the equation.

a)  $x^2 - 8x + 17 = -4$

$$D = b^2 - 4ac$$

$$x^2 - 8x + 17 = 0$$

$$= (-8)^2 - 4(1)(17)$$

$$a = 1$$

$$b = -8$$

$$c = 17$$

$$D = -4 < 0$$

2 imag. solutions

$$\text{b) } x^2 - 8x + 16 = 0$$

$$a = 1 \quad D = (-8)^2 - 4(1)(16)$$

$$b = -8 \quad = 64 - 64$$

$$c = 16 \quad D = 0$$

1 real

$$\text{c) } 8x^2 - 2x + 1 = x^2 + 6$$

$$7x^2 - 2x - 5 = 0 \quad (7x + 5)(x - 1)$$

$$a = 7$$

$$b = -2$$

$$c = -5$$

$$D = (-2)^2 - 4(7)(-5)$$

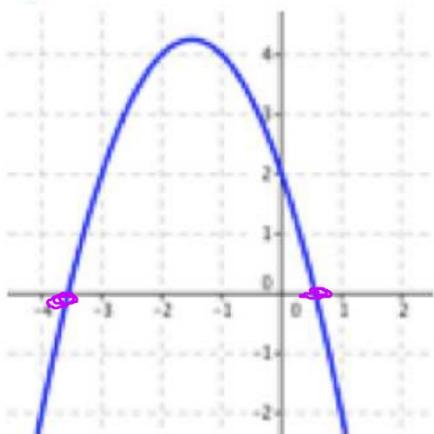
$$= 4 + 140$$

$$= 144 > 0$$

2 real

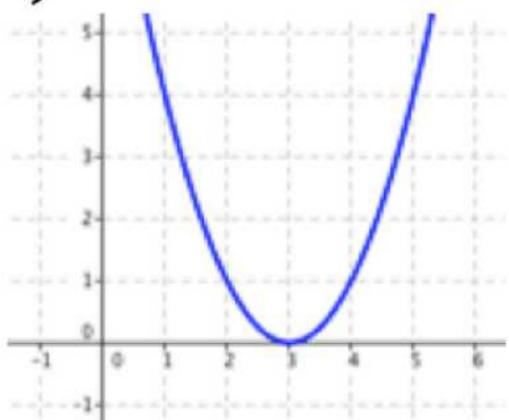
ex: The graph of  $y = ax^2 + bx + c$  or the solutions of  $ax^2 + bx + c = 0$  are given. Determine if the discriminant is positive, negative, or zero. Explain your reasoning.

a)



2 real  
 $D > 0$

b)



|real|

$$\mathcal{D} = \mathbb{O}$$

$$c) x = 2 \pm 3i$$

2 imaginary

$$D < 0$$

(negative)

ex: Consider the quadratic equation:  $3x^2 + 12x + c = 0$

Find all values of  $c$  for which the equation has...  $\frac{3}{3}$

a) two real solutions

$$a = 3 \quad b = 12$$

$$D > 0$$

$$b^2 - 4ac > 0$$

$$144 - 12c > 0$$

$$\frac{-12c}{-12} > \frac{-144}{-12}$$

$$c < 12$$

b) one real solution

$$b^2 - 4ac = 0$$

$$144 - 12c = 0$$

$$c = 12$$

c) two imaginary solutions

$$\begin{aligned}b^2 - 4ac &< 0 \\144 - 12c &< 0 \\c &> 12\end{aligned}$$

## Review

ex:  $y = -(x - 3)(x + 1)$

a) Sketch.

b) State the domain and range in interval notation.

c) What is the maximum or minimum value?

## Review

ex: Which number sets does the number belong to?

$$\sqrt{8}$$

**Review**

**ex: Solve.**

$$9x^2 - 12x = 0$$

Challenge! :)

ex: Solve  $ax^2 + bx + c = 0$  by completing the square.