

$$y = f \cdot g$$
$$y' = f \cdot g' + g \cdot f'$$

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③  $h(t) = \sqrt{t} (1-t^2)$

$$h(t) = t^{1/2} - t^{5/2}$$
$$h'(t) = \frac{1}{2} t^{-1/2} - \frac{5}{2} t^{3/2}$$

$$17.) f(x) = x^f \cos x^g \quad c = \frac{\pi}{4}$$

$$f'(x) = x(-\sin x) + \cos x \cdot 1$$

$$f'\left(\frac{\pi}{4}\right) = \frac{\pi}{4} \left(-\frac{\sqrt{2}}{2}\right) + \frac{\sqrt{2}}{2}$$
$$= \frac{-\sqrt{2}\pi}{8} + \frac{\sqrt{2}}{2}$$

$$53.) \quad y = \overbrace{2x}^f \overbrace{\sin x}^g + \overbrace{x^2}^f \overbrace{\cos x}^g$$

$$y' = \underline{2x(\cos x)} + \sin x \cdot 2 + x^2(-\sin x) + \underline{\cos x \cdot 2x}$$

$$y' = 4x \cos x + 2 \sin x - x^2 \sin x$$

## 2.3 continued The Quotient Rule

$$\frac{d}{dx} \left[ \frac{f}{g} \right] = \frac{g \cdot f' - f \cdot g'}{g^2}$$

$$\frac{d}{dx} \left[ \frac{H_i}{L_o} \right] = \frac{L_o \cdot dH_i - H_i \cdot dL_o}{L_o^2}$$

#1

$$f(x) = \frac{5x+4}{x+2}$$

$$f'(x) = \frac{(x+2)5 - (5x+4) \cdot 1}{(x+2)^2}$$

$$= \frac{5x+10-5x-4}{(x+2)^2}$$

$$f'(x) = \frac{6}{(x+2)^2}$$

$$\#2 \quad f(x) = \frac{\cos x}{x^2}$$

$$f'(x) = \frac{x^2(-\sin x) - \cos x(2x)}{x^4}$$

$$= \frac{-x(x \sin x + 2 \cos x)}{x^4}$$

$$f'(x) = \frac{-(x \sin x + 2 \cos x)}{x^3}$$

$$\#3 \quad h(s) = \frac{s}{\sqrt{s}-1} \quad h(x) = \frac{x}{\sqrt{x}-1}$$

$$h'(x) = \frac{(x^{1/2}-1) \cdot 1 - x^{1/2} \cdot \frac{1}{2} x^{-1/2}}{(\sqrt{x}-1)^2}$$

$$\frac{\frac{1}{2}}{1} = \frac{1}{2}$$

$$\begin{aligned} h'(x) &= \frac{x^{1/2} - 1 - \frac{1}{2} x^{1/2}}{(\sqrt{x}-1)^2} = \frac{\frac{1}{2} x^{1/2} - \frac{2}{2}}{(\sqrt{x}-1)^2} \\ &= \frac{\frac{1}{2} (x^{1/2} - 2)}{(\sqrt{x}-1)^2} = \frac{1(\sqrt{x}-2)}{2(\sqrt{x}-1)^2} \end{aligned}$$

#4 Find  $f'(c)$

$$f(x) = \frac{x+5}{x-5}$$

$$c = 4$$

$$f'(x) = \frac{(x-5) \cdot 1 - (x+5) \cdot 1}{(x-5)^2}$$

$$\begin{aligned} f'(4) &= \frac{-10}{(4-5)^2} \\ &= -10 \end{aligned}$$



#5 Find  $f'(c)$

$$f(x) = \frac{\sin x}{x}$$

$$c = \frac{\pi}{6}$$

$$f'(x) = \frac{x \cdot \cos x - \sin x \cdot 1}{x^2}$$

$$f'\left(\frac{\pi}{6}\right) = \frac{\frac{\pi}{6} \cdot \frac{\sqrt{3}}{2} - \frac{1}{2}}{\frac{\pi^2}{36}} = \left(\frac{\frac{\pi\sqrt{3}}{12} - \frac{1}{2}}{\frac{\pi^2}{36}}\right) \cdot \frac{36}{\pi^2}$$
$$\frac{\pi\sqrt{3} - 6}{12} \cdot \frac{36}{\pi^2}$$
$$\frac{3(\pi\sqrt{3} - 6)}{\pi^2}$$

#6 Find an equation of the tangent line to  $f(x)$  at the given point

$$f(x) = \frac{(x-1)}{(x+1)}, \quad \left(2, \frac{1}{3}\right)$$

$$f'(x) = \frac{(x+1) - (x-1)}{(x+1)^2}$$

$$f'(x) = \frac{2}{(x+1)^2}$$

$$y - \frac{1}{3} = \frac{2}{9}(x-2)$$

$$f'(2) = \frac{2}{9}$$

#7 Find the points where  $f(x)$  has a horizontal tangent

$$f(x) = \frac{x^2}{x^2 + 1}$$

$$f'(x) = \frac{(x^2+1)2x - (x^2)(2x)}{(x^2+1)^2}$$

$(0, 0)$

$$f'(x) = \frac{2x^3 + 2x - 2x^3}{(x^2+1)^2}$$

$$f'(x) = \frac{2x}{(x^2+1)^2}$$

$$0 = \frac{2x}{(x^2+1)^2}$$